Some important numerical problems on electromagnetic induction

The following questions deal with the basic concepts of this section. Answer the following briefly. Go to the next section only if your score is at least 80%. Do not consult the Study Material while attempting these questions.

- **1.** For the circuit shown above the switch is closed at $t = 0$, find
	- (a) the initial current through each resistor.
	- (b) steady state current through each resistor.
	- (c) final energy stored in the capacitor.

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- **2.** A solenoid has an inductance of 10 henry and *a* resistance of 2 ohms. It is connected to a 10 volt battery. The time taken for the magnetic energy to reach 4 $\frac{1}{4}$ th of its maximum value is *x* log_e2 sec. Find the value of *x*?
- **3.** For the circuit shown, the switch *S* is closed at $t = 0$, find (a) the initial current through each resistor. (b) steady state current through each resistor (c) final energy stored in the inductor. $-12V$ 1Ω

4. (a) In a R-L series circuit, the value of resistance is doubled. What is the change in the time constant?

(b) In a R-C series circuit, the value of resistance is doubled, what is the change in time constant?

5. A charged capacitor has energy $E = 10 \mu J$ stored in it. It is connected to an inductor. What is the maximum energy stored in the inductor?

ANSWERS TO PROFICIENCY TEST - I

- **1.** (a) 1A, 2A (b) 1 A, 0 (c) $100 \mu J$
- **2.** 5
- **3.** (a) 6 A, 0, 6A (b) 8A, 4A, 4A (c) 8 J
- **4.** (a) becomes half (b) becomes double
- $5. 10 \text{ uJ}$

Illustration **4**

 $V = 220 \sqrt{2}$

Question: **If the voltage (in volts) in an ac circuit is represented by the equation,**

sin (314 *t* **-), (where** *t* **is in seconds)**

Calculate (a) peak and rms value of the voltage (b) frequency of ac. *Solution:* (a) For *ac* voltage, $V = V_0 \sin{(\omega t - \phi)}$ The peak value

$$
V_0 = 220 \sqrt{2} = 311 \text{ V},
$$

The rms value of voltage

$$
V_{\rm rms} = \frac{V_0}{\sqrt{2}} \; ; \; V_{\rm rms} = 220 \; \text{V}
$$

(b) As $\omega = 2\pi f$, $2\pi f = 314$

i.e.,
$$
f = \frac{314}{2 \times \pi} = 50 \text{ Hz}
$$

Illustration **5**

Question: The electric current in a circuit is given by $i = i_0$ (t/T) for some time. Calculate the rms current for

the period
$$
t = 0
$$
 to $t = T$ for $i_0 = 20\sqrt{3}$ A.

Solution: The mean square current is

$$
\left(\dot{t}^2\right)_{\text{avg}} = \frac{1}{T} \int\limits_0^T \dot{t}_0^2 \left(\frac{t}{T}\right)^2 \, dt = \frac{\dot{t}_0^2}{T^3} \int\limits_0^T \dot{t}^2 \, dt = \frac{\dot{t}_0^2}{3}
$$

Thus, the rms current is

i

$$
i_{\rm rms} = \sqrt{\vec{I}_{\rm avg.}^2} = \frac{\vec{I}_0}{\sqrt{3}} = 20 \text{ A}
$$

Illustration **6**

Question: **An alternating voltage of 100 volt r.m.s. at a frequency of 400/ cycles/second is supplied to a circuit containing a pure inductance of 0.01 H and a pure resistance of 6 ohms in series. Calculate (i) the current, (ii) potential difference across the resistance, (iii) potential difference across the inductance.**

- **Solution:** The impedance of *L-R* series circuit is given by $Z = [R^2 + (\omega L)^2]^{1/2} = [(R)^2 + (2\pi fL)^2]^{1/2} = 10$ Ω (i) R.M.S. value of current $I_{\text{rms}} = \frac{\varepsilon_{\text{rms}}}{7} =$ *Z* $\frac{rms}{2}$ = 10 amp
	- (ii) The potential difference across the resistance is given by $V_R = I_{rms} \times R = 60 \text{ V}$ (iii) Potential difference across inductance is given by
		- $V_L = I_{rms} \times (0/L) = 80 V$

Illustration **7**

Question: **An A.C. source of angular frequency is fed across a resistor** *R* **and a capacitor** *C* **in series. The current registered is** *i***. If now the frequency of the source is changed to /3 (but maintaining the** same voltage), the current in the circuit is found to be halved. The ratio of reactance of resistance at the original frequency is $\sqrt{x} \times 10^{-1}$. Find the value of x?

Solution: At angular frequency ω , the current in *R-C* circuit is given by ϵ

$$
i_{\rm rms} = \frac{\epsilon_{\rm rms}}{\sqrt{\{R^2 + (1/\omega^2 C^2)\}}}
$$
 ... (i)

When frequency is changed to $\omega/3$, the current is halved. Thus

$$
\frac{i_{\text{rms}}}{2} = \frac{\varepsilon_{\text{rms}}}{\sqrt{\left\{R^2 + 1/(\omega/3)^2 C^2\right\}}} = \frac{\varepsilon_{\text{rms}}}{\sqrt{\left\{R^2 + (9/\omega^2 C^2)\right\}}} \qquad \dots (ii)
$$

From equation (i) and (ii), we have

$$
\frac{1}{\sqrt{\{R^2+(1/\omega^2C^2)\}}}=\frac{2}{\sqrt{\{R^2+(9/\omega^2C^2.)\}}}
$$

Solving this equation, we get $3R^2 = \frac{3}{\omega^2 C^2}$ 5 ω^2 *C*

Hence, the ratio of reactance to resistance is $\frac{(1.000)}{2} = 1$ J $\left(\frac{3}{2}\right)$ \setminus $\frac{\omega C}{2}$ = **5 3** *R* $\frac{(1/\omega C)}{2} = \sqrt{\frac{3}{2}}$ \Rightarrow x = 6

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Some important numerical problems on electromagnetic induction

 $Z = j\omega L + Z'.$

where *Z'* is complex impedence due to *C* and *R* in parallel and is given by

$$
\frac{1}{Z} = \frac{1}{R} + j\omega C = \frac{1 + j\omega CR}{R}
$$

or

$$
Z' = \frac{R}{1 + j\omega CR} = \frac{R(1 - j\omega CR)}{1 + \omega^2 C^2 R^2}
$$

$$
\therefore Z = j\omega L + \frac{R(1 - j\omega CR)}{1 + \omega^2 C^2 R^2}
$$

$$
= \frac{R}{1+\omega^2 C^2 R^2} + j \left(\omega L - \frac{\omega C R^2}{1+\omega^2 C^2 R^2}\right)
$$

The magnitude of Z is thus given by

$$
Z = \sqrt{\left[\frac{R^2}{(1 + \omega^2 C^2 R^2)^2} + \left(\omega L - \frac{\omega C R^2}{1 + \omega^2 C^2 R^2} \right)^2 \right]}
$$

or
$$
Z^2 = \frac{R^2}{(1 + \omega^2 C^2 R^2)^2} + \omega^2 L^2 + \frac{\omega^2 C^2 R^4}{(1 + \omega^2 C^2 R^2)^2} - \frac{2 \omega^2 L C R^2}{1 + \omega^2 C^2 R^2}
$$

$$
= \frac{R^2 - 2 \omega^2 L C R^2}{1 + \omega^2 C^2 R^2} + \omega^2 L^2
$$

The peak value of current will be independent of *R*, if *Z* or *Z* 2 is also independent of *R*. It is possible when

$$
R^{2} - 2\omega^{2} LCR^{2} = 0,
$$

or
$$
C = 1/2\omega^{2}L = 1 \mu F
$$

a case will arise when resistance in the circuit is zero. The circuit is purely inductive or capacitive.

Illustration **11**

Question: A series *LCR* with $R = 20 \Omega$, $L = 1.5$ H and $C = 35 \mu F$ is connected to a variable frequency 200 V a.c. **supply. When the frequency of the supply equals the natural frequency of the circuit. What is the average power transferred to the circuit in one complete cycle?**

Solution: When the frequency of the supply equals the natural frequency of the circuit, resonance occurs.

$$
Z = R = 20 \text{ ohm}.
$$

$$
i_{rms} = \frac{E_{rms}}{Z} = \frac{200}{20} = 10 A
$$

Z Average power transferred/cycle $P = E_{rms} i_{rms} \cos 0^{\circ} = 200 \times 10 \times 1 = 2000 \text{ watt}$

PROFICIENCY TEST - II

The following questions deal with the basic concepts of this section. Answer the following briefly. Go to the next section only if your score is at least 80%. Do not consult the Study Material while attempting these questions.

- **1.** State whether the following statements are true or false giving reason in brief
	- (a) dc is more dangerous than ac of same rms value.
	- (b) the average value of ac may be zero over half cycle.
- **2.** Define reactance *X* and impedance *Z*. Can these be negative? If yes, when and what does it imply?

Some important numerical problems on electromagnetic induction

- **3.** Can an ac source be connected to a circuit and yet not delivering any power to it? If so under what circumstances?
- **4.** The potential difference *V* across and the current *I* flowing through an ac circuit is given by, $V = 5$ $\cos \omega t$; $I = 2 \sin \omega t$ What is the power dissipated?
- **5.** A 10 ohm electric iron is connected to 120 volt, 60 Hz wall outlet. What is the rms potential difference on the electric iron?
- **6.** What is the inductive reactance of a coil if the current through it is 20 mA and voltage across it is 100 V?
- **7.** The electric current in an ac circuit is given by $i = i_0 \sin \omega t$. What is the minimum time taken by the current to change from its maximum value to the rms value for $\omega = \frac{\pi}{4}$ $\omega = \frac{\pi}{4}$ rad/s.
- **8.** Find the value of an inductance, which should be connected in series with a capacitor of capacitance 5 μ F, a resistance of 10 Ω and an ac source of 50 Hz so that the power factor (PF) of the circuit is unity. (take $\pi^2 = 10$)
- **9.** The voltage and current in a series AC circuit are given by

$$
V = V_0 \cos \omega t
$$
 and $i = i_0 (\cos \omega t + \frac{\pi}{3})$, where $V_0 = 16$ V, $i_0 = 4$ A

What is the power dissipated in the circuit?

ANSWERS TO PROFICIENCY TEST - II

- **1.** (a) False (b) True
- **2.** $X_L = \omega L$, $X_C = \frac{1}{\omega C}$ $=\omega L, X_C = \frac{1}{2}$ Reactance can be negative when $X_C > X_L$. It implies current leads the applied voltage in the circuit.
- **3.** Yes, when the phase difference between voltage and current is 90°
- **4.** Zero, as $\phi = 90^\circ$
- **5.** 120 V
- 6. $5 k\Omega$
- **7.** 1 sec
- **8.** 2 H
- **9.** 16 W

SOLVED OBJECIVE EXAMPLES

Example **1:**

In the adjoining figure, the current in the steady state, in the 2 resistor is (Internal resistance of battery can be neglected.) (a) 0.3 A

- **(b) 0.5 A**
- **(c) 0.7 A**
- **(d) 0.9 A**

*Solution***:**

In the steady state, the condenser, *C*, does not allow any *d*.*c*. to pass through it. Hence, current in the *AB* branch (i.e. 4Ω resistor) = 0. Hence current, i $(i_1 + i_2)$ in the remaining circuit

$$
= \frac{6V}{2.8\Omega + (6/5)\Omega}
$$

$$
= \frac{6V}{4\Omega}
$$

$$
= 1.5 \text{ A}.
$$

This current is divided between the resistors 2 Ω and 3 Ω . Hence, current through the 2 Ω resistor

=
$$
1.5 \times \frac{3}{5} = 0.9 \text{ A.}
$$

(d)

Example **2:**

(d)

A uniformly wound solenoidal coil of self-inductance 1.8×10^{-4} H and resistance 6Ω is broken into two **identical coils. These induction coils are then connected in parallel across a 12 V battery of negligible resistance. The time constant of the circuit is (neglect mutual induction between the coils)**

(a)
$$
\frac{3}{2} \times 10^{-5}
$$
 s (b) 2×10^{-5} s (c) $\frac{20}{3} \times 10^{-4}$ s (d) 3×10^{-5} s

*Solution***:**

 \rightarrow

The inductance of the circuit (*L*) is given by

$$
\frac{1}{L} = \frac{1}{L_1} + \frac{1}{L_2}
$$
, where $L_1 = L_2 = \frac{1.8}{2} \times 10^{-4} H$

$$
L = \frac{L_1}{2} = \frac{1.8}{4} \times 10^{-4} H
$$

Similarly, resistance of the circuit :
$$
R = \frac{Q}{4} = 1.5\Omega
$$

\n
$$
\therefore \text{ time constant}: \tau = \frac{L}{R} = \frac{0.45 \times 10^{-4}}{1.5} = 3 \times 10^{-5} \text{ sec}
$$

$$
\begin{array}{cc} \cdot & \cdot & \cdot & \cdot \end{array}
$$

Example **3:**

The network shown in figure is part of a complete circuit. If at a certain instant, the current is 5 A and is decreasing at the rate 10³ A/s, the $V_B - V_A$ **is
(a) 20 V (b) 15 V** $(a) 20 V$ **(c) 10 V (d) 5 V**

*Solution***:**

Moving from *A* to *B* $V_A - V_B = (1 \times 5) - (15) - (5 \times 10^{-3} \times 10^3)$ $=-15$ V

 $15V$

$$
V_B - V_A = 15 V
$$
; $\frac{di}{dt}$ is negative as *i* decreases with time.
\n \therefore (b)

Example **4:**

If resistance of 100 Ω and inductance of 0.5 henry and capacitance of 10 \times 10⁻⁶ F are connected in **series through 50 Hertz a.c. supply. The impedance is (a) 1.8765 (b) 18.76 (c) 189.5 (d) 101.3 (d)** 101.3**0**

*Solution***:**

Here
$$
R = 100 \Omega
$$
, $L = 0.5$ H, $C = 10^{-5}$ F
\n
$$
X_L = \omega L = 2\pi \nu L = 100 \pi \times 0.5 = 50 \pi
$$
\n
$$
X_c = \frac{1}{\omega C} = \frac{1}{2\pi \nu C} = \frac{1}{2\pi \times 50 \times 10 \times 10^{-6}} = \frac{10^3}{\pi}
$$
\n
$$
Z = \sqrt{R^2 + (X_L - X_C)^2} = \sqrt{(100)^2 + (50\pi - \frac{10^3}{\pi})^2}
$$
\n
$$
= \sqrt{35934.1} = 189.5 \Omega
$$
\n
$$
\therefore \text{(c)}
$$

Example **5:**

(c)

In an L-R circuit, the value of *L* is $\left[\frac{\bullet.4}{\pi}\right]$ $\overline{}$ ╽ I π **0.4 henry and the value** *R* **is 30 ohm. If in the circuit, an alternating emf of 200 V rms value at 50 cycles per second is connected, the impedance of the circuit and current will be**

(a) 11.4 ohm, 17.5 amphere (b) 30 ohm, 6.5 ampere

(c) 40 ohm, 5 amphere (d) 50 ohm, 4 ampere

*Solution***:**

Here
$$
X_L = \omega_L = 2\pi vL = 40 \Omega
$$

\n $R = 30 \Omega$
\n $Z = \sqrt{R^2 + X_L^2} = \sqrt{30^2 + 40^2} = 50 \Omega$
\n $I_{\text{rms}} = \frac{V_{\text{rms}}}{Z} = \frac{200}{50} = 4 \text{ A}$
\n \therefore (d)

Example **6:**

A series *LCR* **circuit is tuned to resonance. The impedance of the circuit now is**

(b) $2^{2} + (\omega L)^{2} + \left(\frac{1}{2}\right)^{2}$ $\overline{}$ $\overline{}$ \perp $\overline{}$ I l L $\overline{}$ $\overline{}$ Ι $\left(\frac{1}{2}\right)$ l ſ R^2 + $(\omega L)^2$ + $\frac{1}{\omega C}$

*Solution***:**

At resonance
\n
$$
(\omega L - \frac{1}{\omega C}) = 0
$$

\nSo impedance (Z) = R
\n \therefore (d)

(d) *R*

Example **7:**

An inductor of inductance 100 mH is connected in series with a resistance, a variable capacitance and an AC source of frequency 2.0 kHz. The value of the capacitance so that maximum current may be drawn into the circuit is

(a) 60 nF (b) 63 nF (c) 65 nF (d) 89 nF

*Solution***:**

This is an LCR series circuit; the current will be maximum when the net reactance is zero. For this,

$$
\frac{1}{\omega C} = \omega L
$$

or,
$$
C = \frac{1}{\omega^2 L} = \frac{1}{4\pi^2 \times (2.0 \times 10^3 \text{ s}^{-1})^2 (0.1 \text{ H})} = 63 \text{ nF}
$$

:. (b)

Example **8:**

In an A.C. circuit, a resistance of $R \Omega$ is connected in series with an inductance L. If phase angle **between voltage and current be 45°, the value of inductive reactance will be**

(a) *R***/4 (b)** *R***/2**

(c) *R* **(d) cannot be found with given data**

*Solution***:**

 $\tan \phi = \tan 45^\circ$ $=\frac{R}{R}$ *XL* $X_L = R$ **(c)**

Example **9:**

An inductor coil joined to a 6 V battery draws a steady current of 12 A. This coil is connected to a capacitor and an AC source of rms voltage 6 V in series. If the current in the circuit is in phase with the emf, the rms current is

(a) 12 A (b) 20 A (c) 8 A (d) 24 A *Solution***:**

The resistance of the coil is $R = \frac{34}{12A}$ *V* 12 $\frac{6V}{34} = 0.5 \Omega$

In this AC circuit, the current is in phase with the emf, this means that the net reactance of the circuit is zero. The impedance is equal to the resistance. i.e., $Z = 0.5$ Ω

The rms current =
$$
\frac{\text{rms voltage}}{Z} = \frac{6V}{0.5 \Omega} = 12 \text{ A.}
$$

\n
$$
\therefore \quad \text{(a)}
$$

Example **10:**

A generator with an adjustable frequency of oscillation is connected to resistance, $R = 100$ **, inductances,** L_1 = 1.7 mH and L_2 = 2.3 mH and **capacitances,** $C_1 = 4 \mu\text{F}$ **,** $C_2 = 2.5 \mu\text{F}$ **and** $C_3 =$ 3.5 μ F. The resonant angular frequency of **the circuit is (a) 0.5 rad/s (b)** 0.5×10^4 **rad/s (c) 2 rad/s** (d) 2 \times 10⁻⁴ rad/s *E Solution***:** $C_{\text{eff}} = C_1 + C_2 + C_3$ $= 4 \mu F + 2.5 \mu F + 3.5 \mu F$ $= 10 \mu F$ $L_{\text{eff}} = L_1 + L_2$ $= 1.7$ mH $+ 2.3$ mH $= 4$ mH Resonance frequency, $\omega =$ *Leff Ceff* $\frac{1}{\sqrt[4]{C_{\text{eff}}}} = \frac{1}{\sqrt{4 \times 10^{-3} \times 10 \times 10^{-6}}}$ 1 \times 10⁻³ \times 10 \times 10⁻ $=$ $\frac{18}{2}$ $\frac{10^4}{9} = 0.5 \times 10^4$ rad/s. **(b)**

Example **11:**

Figure shows an ac generator connected to a "black box" through a pair of terminals. The box contains an *RLC* **circuit whose elements and connections we do not know. Measurements outside the box reveal that** $v(t) = (75 \text{ V}) \sin \omega_d t$ **, and**

 $i(t) = (1.2 \text{ A}) \sin{(\omega_d t + 42^\circ)}$. Which one of the **following statements is correct?**

- **(a) The power factor is sin 42 and the circuit in the box is largely capacitive.**
- **(b) The power factor is cos 42 and the circuit consists of inductors and resistors.**
- **(c) The rate at which the energy delivered to the box by the generator is 66.88 W.**
- **(d) The circuit consists of capacitors and resistors and the rate at which the energy delivered to the box by the generator is 33.4 W.**

*Solution***:**

$$
V(t) = (75 \text{ V}) \sin \omega_d t
$$

$$
i(t) = (1.2 \text{ A}) \sin{(\omega_d t + 42^\circ)}
$$

Since the current leads the voltage by 42° , the circuit consists of resistors and capacitors. The power factor is $\cos 42^\circ$.

The rate at which the energy is delivered to the box by the generator,

$$
P = V_{\text{rms}} \, i_{\text{rms}} \cos \phi
$$

= $\left(\frac{75V}{\sqrt{2}}\right) \frac{(1.2A)}{\sqrt{2}} \cos 42^\circ = 33.4 \text{ W}$

(d)

Example **12:**

Which of the following plots may represent the reactance of the series LC combination? (a) 1 (b) 3 (c) 2 (d) 4

*Solution***:**

Since
$$
X_{LC} = \omega L - \frac{1}{\omega C}
$$

\n \therefore (d)

Example **13:**

In *RLC* **circuit, at a frequency , the potential difference across each device are** $(\Delta V_R)_{\text{max}} = 8.8 \text{ V}$, $(\Delta V_L)_{\text{max}} = 2.6 \text{ V}$ and $(\Delta V_C)_{\text{max}} = 7.4 \text{ V}$. The combined potential difference $(\Delta V_L + \Delta V_C)_{\text{max}}$ across the inductor and capacitor is
(a) 10 V (b) 7.8 V (c) 7.4 V **(a) 10 V (b) 7.8 V (c) 7.4 V (d) 4.8 V**

*Solution***:**

A phasor representing the alternating current and potential differences across the resistor, capacitor and inductor in the *RLC* circuit.

$$
X_c > X_L
$$

$$
Cos\emptyset = +Ve
$$

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In the steady state, there is no current in the circuit. Hence the points *P* and *Q* are at the same potential as points *A* and *C*. Similarly the potential between *L* and *M* is the same as that between points *P* and *Q*. The capacitance across LM is $\frac{9}{2} \mu F$ $\frac{3}{5} \mu$ F. Hence the charge

P

 20Ω

 W

 1_uF

L M

3 2 μF

100 V

 10Ω *Q*

$$
Q = CV = \frac{3}{2} \times 10^{-6} \times 100 = 150 \times 10^{-6} \text{ C}
$$

100 V

C

 20Ω

A

The charge on each of the 6 μ F and 2 μ F is also 150 \times 10⁻⁶ C since they are connected in series. Thus the potential difference between *A* and *B* is equal to that between the plates of 6 μ F capacitance carrying the charge *Q*.

Hence the potential difference $V_{AB} = \frac{Q}{64} = \frac{188 \times 10^{-6}}{64.0^{-6}}$ 6 6×10 150 × 10 6μ F $6\times10^{-}$ Ē $\dot{\times}$ $=$ $\frac{150 \times}{250}$ įμ $=$ *F* $V_{AB} = \frac{Q}{C_1 F} = \frac{150 \times 10^{-6}}{C_1 40^{-6}} = 25 \text{ V}$

Example **2:**

In an oscillating LC circuit, the energy is shared equally between the electric and magnetic fields. If *L* $= 12$ mH and $C = 1.7$ µF, how much time (in us) is needed for this condition to arise, assuming an **initially fully charged capacitor.**

Solution:

Total energy U_E =

$$
\frac{1}{2}U_{E,\text{max}}
$$

$$
\Rightarrow \qquad \frac{q^2}{2C} = \frac{1}{2}\frac{Q^2}{2C} \Rightarrow q = \frac{Q}{\sqrt{2}}
$$

Since, at $t = 0$, it is given that *C* has maximum charge, we have the solution to be

$$
q = Q \cos \omega t \implies \frac{Q}{\sqrt{2}} = Q \cos \omega t
$$

\n
$$
\implies \omega t = 45^\circ = \frac{\pi}{4} \text{ rad}
$$

\n
$$
\omega = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{(12\times10^{-3})(1.7\times10^{-6})}} = 7 \times 10^3 \text{ rad/s}
$$

\n
$$
\therefore \text{ required } t = \frac{\omega t}{\omega} = \frac{(\pi/4)}{(\pi \times 10^3)} = 1.12 \times 10^{-4} \text{ s}
$$

\n
$$
\implies t = 112 \text{ }\mu\text{s}
$$

Example **3:**

If a direct current of value $a = 1$ ampere is superimposed on an alternating current $I = b \sin \omega t$, when *b* **= 4A, flowing through a wire, what is the effective value of the resulting current in the circuit?**

*Solution***:**

As current at any instant in the circuit will be, $I = I_{dc} + I_{ac} = a + b \sin \omega t$

So,
$$
I_{\text{eff}} = \begin{bmatrix} \frac{1}{2}f^2 dt \\ \frac{1}{2} dt \\ 0 \end{bmatrix}^{1/2} = \left[\frac{1}{T}\int_0^T (a + b\sin\omega t)^2 dt\right]^{1/2}
$$

i.e.,
$$
I_{\text{eff}} = \left[\frac{1}{T}\int_0^T (a^2 + 2ab\sin\omega t + b^2 \sin^2 \omega t) dt\right]^{1/2}
$$

 $10²$

but as

 $\varsigma_{\textnormal{o}}$

$$
\frac{1}{T} \int_{0}^{T} \sin \omega t \, dt = 0 \text{ and } \frac{1}{T} \int_{0}^{T} \sin^{2} \omega t \, dt = \frac{1}{2}
$$

$$
I_{\text{eff}} = \left[a^{2} + \frac{1}{2} b^{2} \right]^{1/2} = 3A
$$

Example **4:**

A 12 ohm resistance and an inductance of $0.05/\pi$ henry with negligible resistance are connected in **series. Across the end of this circuit is connected a 130 volt alternating voltage of frequency 50 cycles/second. Calculate the potential difference across the inductance.**

*Solution***:**

The impedance of the circuit is given by

$$
Z = \sqrt{(R^2 + \omega^2 L^2)} = \sqrt{[R^2 + (2\pi L)^2]}
$$

= $\sqrt{[(12)^2 + (2 \times 3.14 \times 50 \times (0.05/3.14))^2]} = \sqrt{(144 + 25)} = 13 \text{ ohm}$

Current in the circuit $i = E/Z = \frac{1}{13}$ $\frac{130}{12}$ = 10 amp.

Inductive reactance of coil $X_L = \omega L = 2\pi fL$

$$
\therefore \qquad X_L = 2\pi \times 50 \times \left(\frac{0.05}{\pi}\right) = 5 \text{ ohm}.
$$

Potential difference across inductance

 $V_L = i \times X_L = 10 \times 5 = 50$ volt.

Example **5:**

A resistance of 10 ohm is joined in series with an inductance of 0.5 henry and a capacitor to obtain maximum current. What will be the potential difference across the inductance. The current is being supplied by 200 volts and 50 rad/s per second mains.

*Solution***:**

The current in the circuit would be maximum when

$$
\omega L = \frac{1}{\omega C}
$$
 or $C = \frac{1}{\omega^2 L}$

Here $\omega L = 1/\omega C$. So the impedance *Z* of the circuit

$$
Z = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2} = R = 10 \text{ ohm}
$$

$$
I = \frac{E}{R} = \frac{200}{10} = 20 \text{ amp.}
$$

Potential difference across inductance

$$
V_L = \omega L \times I = 500
$$
 V

Example **6:**

A 100 volt a.c. source of frequency 500 hertz is connected to *LCR* **circuit with** *L* **= 8.1 milli**henry, $C = 12.5$ microfarad and $R = 10$ ohm, all connected in series. Find the potential difference **across the resistance.**

*Solution***:**

The impedance of LCR circuit is given by

$$
Z = \sqrt{[R^2 + (X_L - X_C)^2]}
$$

where $X_I = \omega L = 2\pi fL$

$$
= 2 \times 3.14 \times 500 \times (8.1 \times 10^{-3}) = 25.4 \text{ ohm}
$$

and
$$
X_C = \frac{1}{\omega C} = \frac{1}{2\pi fC} = \frac{1}{2.3.14 \times 400 \times (12.5 \times 10^{-6})} = 25.4 \text{ ohm}
$$

∴
$$
Z = \sqrt{[(10)^2 + (25.4 - 25.4)^2]} = 10 \text{ ohm}
$$

∴
$$
I_{\text{rms}} = \frac{E_{\text{rms}}}{Z} = \frac{100 \text{volt}}{10 \text{ ohm}} = 10 \text{ amp.}
$$

Potential difference across resistance

 $V_R = I_{\text{rms}} \times R = 10 \text{ amp} \times 10 \text{ ohm}$ = **100 volt.**

Example **7:**

An *LCR* series circuit with 100 Ω resistance is connected to an AC source of 200 V and angular **frequency 300 radians per second. When only the capacitance is removed, the current lags behind the voltage by 60°. When only the inductance is removed, the current leads the voltage by 60°. Calculate power dissipated in** *LCR* **circuit.**

*Solution***:**

$$
\tan 60^\circ = \frac{\omega L}{R} \text{ or } \tan 60^\circ = \frac{1/\omega C}{R}
$$

 $\overline{}$ $\overline{}$ $\overline{}$

I J

 $\left(\omega L - \frac{1}{2}\right)$

Y ſ $+\alpha L - \omega$ $2\left(\begin{matrix} 2 \\ 0 \end{matrix}\right)^2$ R^2 + $\left(\omega L - \frac{1}{\omega C}\right)$ = R

 $\overline{}$

$$
\therefore \qquad \omega L = \frac{1}{\omega C}
$$

Impendance of circuit *Z* =

Current in the circuit

$$
I_0 = \frac{V_0}{Z} = \frac{V_0}{R} = \frac{200}{100}
$$

= 2 Amp.

Average power $P = \frac{1}{2}$ $\frac{1}{2}$ *V*₀*I*₀ cos φ

But,
$$
\tan \phi = \frac{\omega L - (1/\omega C)}{R} = 0
$$
 (cos $\phi = 1$)

L \mathbf{r} L

I

Now,
$$
\overline{P} = \frac{1}{2} \times 200 \times 2 \times 1 = 200
$$
 watt.

Example **8:**

A current of 4 A flows in a coil when connected to a 12 V d.c. source. If the same coil is connected to a 12 V, 50 rad/s, a.c. source, a current of 2.4 A flows in the circuit. The inductance of the coil is $x \times 10^{-2}$ **H. Find** *x***.**

*Solution***:**

When the coil is connected to a d.c. source, its resistance *R* is given by

$$
R=\frac{V}{I}=\frac{12}{4}=3\ \Omega
$$

When it is connected to a.c. source, the impedance *Z* of the coil is given by

$$
Z = \frac{V_{rms}}{I_{rms}} = \frac{12}{2.4} = 5\Omega
$$

coil,
$$
Z = \sqrt{[R^2 + (\omega L)^2]}
$$

For a coil, 2

$$
\therefore \qquad 5 = \sqrt{[(3)^2 + (50L)^2]}
$$

or
$$
25 = [(3)^2 + (50L)^2]
$$

Solving we get $L = 0.08$ henry \Rightarrow **x** = 8

Example **9:**

For a resistance $R = 100 \Omega$ and capacitance $C = 100 \mu F$ in series, the impedence is twice that of a **parallel combination of the same elements. What is the angular frequency of applied emf?**

*Solution***:**

As shown in figure (a), in case of series combination,

$$
Z_{s} = \sqrt{R^{2} + X_{C}^{2}} = [R^{2} + (1/\omega C)^{2}]^{1/2}
$$

In case of parallel combination,

$$
I_R = \frac{V}{R} \sin \omega t \text{ and } I_C = \frac{V}{X_C} \sin \left(\omega t + \frac{\pi}{2} \right)
$$

C V X

So,
$$
I = I_R + I_C = \frac{V}{R}\sin\omega t + \frac{V}{X_C}\cos\omega t
$$

i.e.,
$$
I = I_0 \sin{(\omega t + \phi)}
$$

with $I_0 \cos \phi = \frac{V}{R}$ $\frac{V}{R}$ and *I*₀ sin ϕ =

So,
$$
I_0 = \left[\left(\frac{V}{R} \right)^2 + \left(\frac{V}{X_C} \right)^2 \right]^{1/2} = \frac{V}{Z_P}
$$

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i.e.,
$$
\frac{1}{Z_P} = \left[\frac{1}{R^2} + \left(\frac{1}{X_C} \right)^2 \right]^{1/2}
$$

\ni.e., $Z_P = \frac{R}{\sqrt{1 + \omega^2 C^2 R^2}}$
\nand as according to given problem,
\n $Z_s = 2Z_P$, i.e., $Z_s^2 = 4Z_P^2$
\ni.e., $\frac{(R^2 \omega^2 C^2 + 1)}{\omega^2 C^2} = 4 \frac{R^2}{(1 + R^2 \omega^2 C^2)}$
\ni.e., $(1 + R^2 \omega^2 C^2)^2 = 4R^2 \omega^2 C^2$
\nor, $1 + R^2 \omega^2 C^2 = 2R \omega C$
\nor, $(R \omega C - 1)^2 = 0$
\nor, $\omega = \frac{1}{RC}$,
\n $\omega = 100 \text{ rad/s}$

MIND MAP

$$
\frac{1}{\sqrt{l}}
$$

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MIND MAP

EXERCISE – I

CBSE PROBLEMS

- **1.** What is iron loss in a transformer?
- **2.** Sketch a graph to show how the reactance of (i) a capacitor (ii) an inductor varies as a function of frequency?
- **3.** A capacitor blocks d.c. and allows a.c. Why?
- **4.** A bulb connected in series with a solenoid is lit by a.c. source. If a soft iron core is introduced in the solenoid, will the bulb glow brighter?
- **5.** Derive an expression for the average power over a complete cycle of a.c. in a non-inductive circuit.
- **6.** What is meant by r.m.s. value of a.c.? Derive an expression for r.m.s. value of alternating current and emf.
- **7.** Give the principle, construction, theory and working of an a.c. generator.
- **8.** The core of a transformer is laminated, why?
- **9.** When a current flows in the coil of a transformer, then why does its core become hot?
- 10. What is the maximum value of power factor? When does it occur?

EXERCISE – II

NEET-SINGLE CHOICE CORRECT

(a) 5000 (b) 50 (c) 500 (d) 5

- **12.** In an AC circuit, a resistance of *R* ohm is connected in series with an inductance *L*. If phase difference between voltage and current be 45° , the value of inductive reactance will be (a) $R/4$ (b) $R/2$ (c) *R* (d) cannot be found with the given data
- **13.** A coil has an inductance of 0.7 H and is joined in series with a resistance of 220Ω . An alternating emf of 220V at 50 Hz is applied to it. Then the wattless component of the current in the circuit is (a) 5 amp (b) 0.5 amp (c) 0.7 amp (d) 7 amp
- **14.** The voltage and current in a series *AC* circuit are given by $V = V_0 \cos \omega t$ and $I = I_0 (\cos \omega t +$ 3 π). What is the power dissipated in the circuit?
	- (a) 2 $V_0 I_0$ (b) 0 (c) 4 $V_0 I_0$ (d) $\frac{\sqrt{6}}{2}V_0I_0$ $\frac{3}{5}V_0$
- **15.** The network shown in the figure is part of a complete circuit. If at a certain instant, the current *I* is 10 *A*, and is decreasing at a rate 10^3 A/s then $V_A - V_B$ is

1 15V 1 5mH *A B I* + 5V + (a) 20 V (b) 15 V (c) 10 V (d) 5 V

16. In the circuit of figure, what will be the reading of the voltmeter? (a) 300 V (b) 900 V (c) 200 V (d) 400 V

17. In a circuit shown in figure, what will be the readings of the voltmeter and ammeter if a.c. source of 200 V and 50 Hz is connected (a) 800 V, 2 A (b) 300 V, 2 A (c) 200 V, 2 A (d) 100 V, 2 A

18. The root-mean-square value of an alternating current of 50 Hz frequency is 10 A. The time taken by the alternating current in reaching from zero to maximum value and peak value will be (a) 2×10^{-2} s and 14.14 A (b) 1×10^{-2} (b) 1×10^{-2} s and 7.07 A (c) 5×10^{-3} s and 7.07 A (d) 5×10^{-3} (d) 5×10^{-3} s and 14.14 A

19. A 120 volt AC source is connected across a pure inductor of inductance 0.70 Henry. If the frequency of the source is 60 Hz, the current passing through the inductor is (a) 4.55 A (b) 0.325 A (c) 0.455 A (d) 3.25 A

20. In a *LCR* circuit capacitance is changed from *C* to 2*C*. For the resonant frequency to remain unchanged, the inductance should be changed from *L* to (a) $4 L$ (b) $2 L$ (c) *L*/2 (d) *L*/4

- **21.** An alternating current flows through a circuit consisting of inductance *L* and resistance *R*. Periodicity of the supply is $\omega/2\pi$. Which of the following is true? (a) the limiting value of impedance is *L* for low frequency
	- (b) the limiting value of impedance for low frequency is *R*
	- (c) limiting value of impedance for high frequency is *R*
	- (d) the limiting value of impendence for low frequency is *L*

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22. The charge on either plate of the capacitor *C* as shown in the figure is

(a) *CE*
\n(b)
$$
\frac{CER_1}{R_2 + r}
$$
\n(c)
$$
\frac{CER_2}{R_2 + r}
$$
\n(d)
$$
\frac{CER_1}{R_1 + r}
$$

(d) $P = P'$

23. Alternating current cannot be measured by D.C. ammeter because

(a) A.C. can not pas through D.C. Ammeter

(b) A. C. changes direction

- (c) Average value of current for complete cycle is zero
- (d) D.C. Ammeter will get damaged
- **24.** In a series R-L-C AC circuit, for a particular value of *R*, *L* and *C*, power supplied by the source is *P* at resonance. If the value of inductance is halved, then the power from the source again at resonance is *P*' . Then

(a)
$$
P = \frac{P'}{2}
$$
 (b) $P = 2P'$ (c) $P = 4P'$

25. In a circuit, capacitor $(C = 4 \mu F)$ is connected in series with a resistor $(R = 2.5 M \Omega)$ with a battery of 12 V having negligible internal resistance. Find the time after which potential difference across capacitor becomes three times of potential difference across resistor (ln2 = 0.693). (a) 13.86 s (b) 1.386 s (c) 6.93 s (d) 20 s

EXERCISE – III

IIT-JEE- SINGLE CHOICE CORRECT

- 1. A capacitor of capacitance 10μ F is charged to a potential of 1V. It is connected in parallel to an inductor of inductance 10^{-3} H. The maximum current that will flow in the circuit has the value (a) 1 uA (b) 1 mA (c) $\sqrt{1000}$ mA (d) 100 mA
- **2.** An inductor *L* and a capacitor *C* are connected in the circuit as shown in the figure. The frequency of the power supply is equal to the resonant frequency of the circuit. Which ammeter will read zero ampere? (a) A_1 (b) A_2

3. The magnitude of currents in different branches are shown in the circuit. Then (a) $I = I_L + I_C$ if inductor and capacitor are pure (b) $I = I_L - I_C$ if inductor and capacitor are pure (c) $I = I_L + I_C$ if inductor and capacitor are not pure

(d) $I = I_L - I_C$ if inductor and capacitor are not pure

4. Two resistors of 10 Ω and 20 Ω and an ideal inductor of 10 H are connected to a 2 V battery as shown in figure. At time $t = 0$, key *K* is closed. Then the initial and final currents through the battery are

(a)
$$
\frac{1}{15}A, \frac{1}{10}A
$$

\n(b) $\frac{1}{10}A, \frac{1}{15}A$
\n(c) $\frac{2}{15}A, \frac{1}{10}A$
\n(d) $\frac{1}{15}A, \frac{2}{25}A$

5. Match List I (expression for current) with List II (rms value of current) and select the correct answer. **List –I List-II** $\mathcal{L}_{\mathcal{A}}$

6. In a region of uniform magnetic induction $B = 10^{-2}$ T, a circular coil of radius 30cm and resistance π^2 ohm is rotated about an axis which is diameter of the coil. If the coil rotates at 200 rpm, the amplitude of the alternating current induced in the coil is (a) $4 \pi^2$ mA ² mA (b) 30 mA (c) 6 mA (d) 200 mA

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- **7.** In the given circuit, the potential difference between point *P* and *Q* in steady state is (a) 40 V (b) 21 V (c) 18 V (d) 18 V 5 *Q* 2Ω 2uF $1H \overline{3}\Omega$ P^{\bullet} ₅ \overrightarrow{AA}
- **8.** A circular coil of radius 0.1 m has 80 turns of wire. If the magnetic field through the coil increases from 0 to 2 tesla in 0.4 sec and the coil is connected to a 11 ohm resistor, what is the current (in A) through the resistor during the 0.4 sec? (a) $(8/7)$ A (b) $(7/8)$ A (c) 8A (d) 7A
- **9.** The primary winding of a transformer has 100 turns and its secondary winding has 200 turns. The primary is connected to an AC supply of 120V and the current flowing in it is 10A. The voltage and the current in the secondary are

(a) 240V, 5A (b) 240V, 10A (c) 60V, 20A (d) 120V, 20A **10.** In the figure, which voltmeter reads zero, when ω is equal to the resonant frequency of series *LCR* circuit? (a) V_1 (b) V_2 (c) V_3 (d) None of these

11. An ideal choke takes a current of 8 ampere when connected to an AC supply of 100 volt and 50Hz. A pure resistor under the same conditions takes a current of 10 ampere. If the two are connected to an AC supply of 150 volt and 40 Hz, then the current in a series combination of the above resistor and inductor is

(a) 10 amp (b) 8 amp (c) 18 amp

 $(15/\sqrt{2})$ amp

12. Current in R_3 just after closing the switch and in steady state respectively, will be

 $(a) 0,0$

 (c) 0, *R*3 *E*

(d) indeterminate

,0 $R₃$ *E*

- **13.** In the circuit shown in the figure at resonance. (a) The power factor is zero (b) The current through the a.c. source is minimum (c) The current through the a.c. source is maximum
	- (d) Currents through *L* and *R* are equal.
- 14. In the circuit shown in figure, the r.m.s. value of e is 5 V and r.m.s. value of voltage drop across L is 3 V. The r.m.s. value of voltage across R will be (a) $2 V$ (b) $3 V$ (c) 4 V (d) 0 V

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14. In the circuit shown in figure, the r.m.s. value of *e* is 5 V and r.m.s. value of voltage drop across *L* is 3 V. The r.m.s. value of voltage across *R* will be (a) 2 V (b) 3 V (c) 4 V (d) 0 V

15. An AC source producing emf $\varepsilon = \varepsilon_0 [\cos (100 \pi s^{-1})t + \cos (500 \pi s^{-1})t]$ is connected in series with a capacitor and a resistor. The steady-state current in the circuit is found to be $i = i_1 \cos \left[(100 \pi s^{-1}) t + \phi_1 \right] + i_2 \cos \left[(500 \pi s^{-1}) t - \phi_2 \right]$, Then (a) $i_1 > i_2$

-
- (b) $i_1 = i_2$ (c) $i_1 < i_2$
- (d) the information is insufficient to find the relation between i_1 and i_2 .

16. In the a.c. circuit shown in figure, the supply voltage has a constant r.m.s. value ε but variable frequency f . Resonance frequency in Hertz is (a) 10 (b) 100

(c) 1000 (d) 200

17. In the circuit shown in figure, the initial value of current through the battery after closing the circuit (i.e., *K* pressed) is

> (a) 0.2 A (b) 0.24 A (c) 0.3 A (d) none of these

18. The plates of a capacitor are charged to a potential difference of 320 volt and are then connected to a resistor. The potential difference across the capacitor decays exponentially with time. After 1sec, the potential difference between the plates of the capacitor is 240 V, then after 2 and 3 seconds potential difference between the plates will be, respectively (a) 200 V and 180 V (b) 180 V and 135 V (c) 160 V and 80 V (d) 140 V and 20 V

19. In the circuit shown in the figure, if value of $R = 60 \Omega$, then the current flowing through the capacitor will be (a) 0.5 A (b) 0.25 A (c) 0.75 A (d) 1.0 A

20. The value of admittance in the adjoining circuit shown in figure is (a) 0.1 mho (b) 0.25 mho (c) 0.35 mho (d) 9.7 mho

21. The reactance of a capacitor X_C in an ac circuit varies with frequency of the source voltage. Which one of the following represents this variation correctly?

f

(d)

X^C

22. For the circuit shown in figure current in inductance is 0.8 A while in capacitance is 0.6 A. What is the current drawn from the source?

(a) 0.2 A (b) 0.4 A (c) 0.6 A (d) 1 A

23. A capacitor is charged through a resistor of resistance *X*. If the resistance is made 2*X* then the graph between log *I* and *t* is (the dotted line represents the initial graph)

(a)
$$
P
$$
 (b) Q (c) R (d) S

24. An inductor ($L = 100$ mH), a resistor ($R = 100 \Omega$) and a battery $(E = 100 \text{ V})$ are initially connected in series as shown in the figure. After a long time the battery is disconnected after short circuiting the points *A* and *B*. The current in the circuit 1 ms after the short circuit is

(a) 1 A (b)
$$
1/e
$$
 A (c) e A

25. The current in 1 Ω resistance and the charge stored in the capacitor are (a) 5 A, 10 μ C (b) 7 A, 12 μ C (c) 4 A , $12 \mu C$ (d) 6 A , $6 \mu C$

f

EXERCISE – IV

ONE OR MORE THAN ONE CHOICE CORRECT

1. Power factor may be one for

(a) pure inductor (b) pure capacitor (c) pure resistor (d) series LCR circuit

- **2.** Current in circuit may be wattless if
	- (a) inductance in the circuit is zero
	- (b) resistance in the circuit is zero
	- (c) current is alternating
	- (d) reactance in the circuit is zero but inductance not zero.
- **3.** Average power in an A.C. circuit is given by
	- (a) $E_{\rm rms} I_{\rm rms} \cos \phi$ (b) $(I_{\rm rms})^2 R$ $(|Z|)'$ 2 2 0 2 |*Z* | E_0^2R (d) 2 $|I_0^2|Z|\cos\phi$
- **4.** In an AC series circuit, the instantaneous current is zero when the instantaneous voltage is maximum. Connected to the source may be
	- (a) pure inductor (b) pure capacitor
	-
-
- (c) pure resistor (d) combination of inductor and capacitor
- **5.** A coil of inductance *L* and resistance *R* is connected across a d.c. source of emf *E* (of negligible internal resistance). The current in the circuit varies with time *t* as shown by curve (a). When one or more of parameters *E*, *R* and *L* are changed, the curve (b) is obtained. Steady state current is same in both the cases. Then possible changes is/are
	- (a) *E* and *R* are kept constant and *L* is increased
	- (b) *E* and *R* are kept constant and *L* is decreased
	- (c) *E* and *R* are both halved and *L* is kept constant
	- (d) *E* and *L* are kept constant and *R* is decreased

6. In the circuit shown

- (a) time constant is *L*/*R*
- (b) time constant is 2*L*/*R*
- (c) steady state current in inductor is 2*E*/*R*
- (d) steady state current in inductor is *E*/*R*

- **7.** In the circuit shown switch *S* is closed at time $t = 0$, initially capacitor is uncharged and initially current through the inductor is zero. Then
	- (a) initial current through capacitor is *E*/2*R*
	- (b) initial rate of rise of current through inductor is *E*/*L*
	- (c) initial current through capacitor is *E*/*R*
	- (d) initial rate of rise of current through inductor is 2*E*/*L*

8. The S.I. unit of inductance Henry can be written as

- (a) weber/ampere (b) volt-sec/ampere
- (c) Joule/ampere² (d) ohm-second

9. If an alternating voltage is given by $e = e_1 \sin \omega t + e_2 \cos \omega t$ the

(a) root mean square value of voltage is $\frac{\sqrt{9}}{2}$ $e_1^2 + e_2^2$

(b) average value of voltage over one time period 2 $e_1 + e_2$

(c) root mean square value of voltage is 2 $e_1^2 + e_2^2$

(d) average value of voltage over one time period is zero

10. A capacitor of capacitance 1μ F is charged to potential difference of 2V and is connected across an inductor of 1 mH. At an instant when potential difference across capacitor is 1V, the current in the circuit is i_1 . The maximum current through inductor is i_0 , then

(a)
$$
i_0 = \sqrt{4000} \text{ mA}
$$

\n(b) $i_0 = \sqrt{2000} \text{ mA}$
\n(c) $i_1 = \sqrt{3000} \text{ mA}$
\n(d) $i_1 = \sqrt{1000} \text{ mA}$

11. An inductive reactance $X_L = 100\Omega$, a capacitive reactance $X_C = 100 \Omega$ and resistance *R* $= 100 \Omega$ are connected in series to an a.c. source of $e = 100 \sin (50 t)$ volts. Which of the following statements is/are correct.

- (a) the maximum voltage across capacitor is 100 volts
- (b) the impedance of the circuit is 100Ω
- (c) the maximum voltage across inductor is 100 volts
- (d) the maximum voltage across the combination is 100 volts
- **12.** A circuit consists of a resistance and capacitance in series. An alternating emf of 180 volts and 100 cycle/sec frequency is applied to it. If rms value of current is 6 amp and power consumed in the resistance is 360 watts then

- (a) circuit impendence is 30 ohms
- (b) capacitive reactance is 100 ohms
- (c) circuit resistance is 10 ohm
- (d) circuit resistance is 20 ohms

13. A circuit has resistance $R = 10 \Omega$ and coil of inductance $L = 15H$ in series. At any instant current flowing through the circuit is $\mathbf{i} = 2t^2 - 4$, then which of the following is/are correct

- (a) voltage across the coil at $t = 1$ sec is 60V
- (b) energy stored in the inductor at $t = 1$ sec is 30 J
- (c) voltage at $t = 2/3$ sec is 60 V
- (d) energy store in the inductor at $t = 2/3$ sec is 30 J

14. An L-C-R series circuit with 100 Ω resistance is connected to an *ac* source. When only the capacitance is removed, the current lags behind voltage by 4 π . When only the inductance is

removed, the current leads voltage by 4 $\frac{\pi}{\cdot}$. Then

- (a) Inductive reactance is 100Ω
- (b) Capacitive reactance is 100Ω
- (c) Impedance of L-C-R circuit is 100Ω

(d) maximum potential difference across inductor is equal to maximum potential difference across capacitor when all are connected in circuit.

15. A leaky parallel plate capacitor is filled completely with a material having dielectric constant $K = 5$ and electrical conductivity σ . If initial charge on the capacitor is q_0 , positive plate and negative plate of capacitor are connected to each other by conducting wire at $t = 0$, then

(a) time constant of the circuit is σ $5\varepsilon_{_0}$

(b) current in the circuit at any time *t* is $\frac{q_0 \sigma}{r} e^{-5\varepsilon_0}$ 0 $\mathbf 0$ 5 ε $-\frac{t\sigma}{\sigma}$ ϵ σ ^{$-\frac{1}{5}$} $\frac{q_0 \sigma}{q}$

(c) current in the circuit at any time *t* is $\frac{900}{5\epsilon_0}$ 1– $e^{-5\epsilon_0}$ $\overline{}$ J \backslash I I \setminus ſ \overline{a} ϵ $\sigma \left(\begin{array}{cc} & -\frac{\sigma t}{5\varepsilon_0} t \end{array} \right)$ $\frac{q_0 \sigma}{2}$ 1 - $e^{-\frac{\sigma^2}{5\varepsilon_0}}$ 0 $\frac{100}{1}$ 1 5

(d) none of these

EXERCISE – V

MATCH THE FOLLOWING

Note: Each statement in column – I has only one match in column –II

1. Questions asked in column –I and answers are given in column-II, match the following

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Note: Each statement in column – I has one or more than one match in column –II.

3. A capacitor of capacity *C* is fully charged with a battery of emf *V*⁰ and connected through an inductor of inductance *L* through two switches S_1 and S_2 respectively as shown in the figure. At $t = 0$, both switches S_1 and S_2 are closed. Given below are two columns. In column I, some conditions related to system and in column II, their corresponding times are given, match the column I with column II.

REASONING TYPE

Directions: Read the following questions and choose

- **(A) If both the statements are true and statement-2** is the correct explanation of **statement-1**.
- **(B) If both the statements are true but statement-2** is not the correct explanation of **statement-1**.
- **(C) If statement-1** is True and **statement-2** is False.
- **(D) If statement-1** is False **and statement-2** is True.

1. Statement-1: A resistance is connected to an ac source. Now a capacitor is included in the circuit. The average power absorbed by the resistance will not be same. **Statement-2**: By including a capacitor or an inductor in the circuit root mean square current and power factor will be changed. (a) (A) (b) (B) (c) (C) (d) (D)

2. Statement-1: In LCR series circuit, power factor can be improved by introducing a capacitor of appropriate capacitance in the circuit.

Statement-2: By adjusting C, the value of *Z* can be made to approach R in ac circuit. (a) (A) (b) (B) (c) (C) (d) (D)

3. Statement-1: Reactances of inductor and capacitor respectively vary linearly and inversely with frequency.

Statement-2: Reactance of inductor and capacitor does not depend on the frequency. (a) (A) (b) (B) (c) (C) (d) (D)

- **4. Statement-1**: In any a.c. series circuit, the applied instantaneous voltage is not equal to the algebraic sum of the instantaneous voltage across the different elements of the circuit. **Statement-2**: The voltage across different elements are not in phase only their phasor sum is equal to the applied voltage. (a) (A) (b) (B) (c) (C) (d) (D)
- **5. Statement-1**: The average power over one complete cycle in a.c circuit cannot be negative. **Statement-2:** A pure inductance or a pure capacitance does not consume average power. (a) (A) (b) (B) (c) (C) (d) (D)

LINKED COMPREHENSION TYPE

EXERCISE – VI

SUBJECTIVE PROBLEMS

- **1.** A coil has a resistance of 10 Ω and an inductance of 0.4 henry. It is connected to an AC source of 6.5 V, π $\frac{30}{\text{Hz}}$ Hz. The average power consumed in the circuit is $x \times 10^{-3}$ W. Find the value of *x*.
- **2.** Find the rms value for the saw-tooth voltage of peak value $V_0 = 10\sqrt{3}$ volts as shown in figure.

3. The series and parallel circuits shown in figure have the same impedance and the same power factor. If *R* $= 3\Omega$ and $X = 4\Omega$. The value of X_1 is $a \times 10^{-2} \Omega$. Find the value of *a*.

4. Find the potential difference $\phi_B - \phi_A$ between the plates of a capacitor *C* in the circuit shown in figure. If the sources have emf's $E_1 = 4.0$ V and $E_2 = 1.0$ V and the resistances are equal to $R_1 = 10 \Omega$, $R_2 = 20 \Omega$, and $R_3 = 30 \Omega$. The internal resistance of the sources are negligible.

5. The voltage across the capacitor C varies with time *t* as $V = a(1-e^{-bt})$ volts as shown in the figure after the shorting of the switch *Sw* at the moment $t = 0$. Calculate the value of $\frac{a}{b}$ $\frac{a}{b}$ in volts – ohm-uF.

at time $t = 0$.

6. A metal rod *OA* of mass m = 1 kg and length $r = \sqrt{2}$ m is rotating with a constant angular speed ω $=\frac{\pi}{2}$ $\frac{\pi}{6}$ rad/s in a vertical plane about a horizontal axis at the end *O*. The free end A is arranged to slide without friction along a fixed conducting circular ring in the same plane as that of rotation. A uniform and constant magnetic induction $\vec{B} = 2T$ is applied perpendicular and into the plane of rotation as shown in the Figure. An inductor $L = 2H$ and an external resistance $R = \pi \Omega$ are connected through a switch *S* between the point *O* and a point *C* on the ring to form an electrical

circuit. Neglect the resistance of the ring and the rod. Initially, the switch is open. Switch is closed

Calculate the torque required to maintain the constant angular speed at $t = \frac{1}{2}$ $\frac{1}{2}$ s (given that the rod *OA* was along the positive *X*-axis at $t = 0$.

7. In the circuit shown the switch *S* is shifted to position 2 from position 1 at *t* = 0, having been in position 1 for a long time. The current in the circuit as a function of time is $I = a-b e^{-ct}$, where a, b and c are constants. $a \times c$

Find the value of
$$
\frac{d \times C}{b}
$$
 in M.K.S.Units

Some important numerical problems on electromagnetic induction

8. In the circuit shown, if the power factor of the circuit is 1 and power factor of box is 5 $\frac{3}{5}$. Calculate the reading of ammeter

9. For the given LCR circuit. Calculate the *Q* factor

10. In the given circuit, $E_1 = 3E_2 = 2E_3 = 6$ V $R_1 = 2R_4 = 6 \Omega$ $R_3 = 2R_2 = 4 \Omega$ $C = 5 \mu F$ Find the charge on the capacitor in steady state.

(voltage gain) of the circuit

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ANSWERS

EXERCISE – II

NEET-SINGLE CHOICE CORRECT

EXERCISE – III

IIT-JEE-SINGLE CHOICE CORRECT

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EXERCISE – IV

MORE THAN ONE CHOICE CORRECT

EXERCISE – V

MATCH THE FOLLOWING

- **1.** $I C$, $II D$, $III A$, $IV B$
- **2.** I D, II C, III B, IV A
3. I B, D, II A, C, III B, D
- **3.** I B, D, II A, C, III B,D, IV A, C

REASONING TYPE

LINKED COMPREHENSION TYPE

Q.10 If instantaneous value of current is $I = 10 \sin(314 t)$ A, then the average current for the half cycle will be -

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- **Q.11** The r.m.s. value of alternating current is 10 amp having frequency of 50 Hz. The time taken by the current to increase from zero to maximum and the maximum value of current will be -
	- (1) 2 \times 10⁻² sec. and 14.14 amp
	- (2) 1 \times 10⁻² sec. and 7.07 amp
	- (3) 5 \times 10⁻³ sec. and 7.07 amp (4) 5 \times 10⁻³ sec. and 14.14 amp
- **Q.12** In a circuit an a.c. current and a d, c. current are supplied together. The expression of the instantaneous current is given as $i = 3 + 6$ sin ωt . Then the rms value of the current is -
	- $(1) 3$ (2) 6 (3) 3 $\sqrt{2}$ (4) 3 $\sqrt{3}$
- **Q.13** The emf and the current in a circuit are
	- $E = 12 \sin(100 \pi t)$;
	- I = 4 sin (100 π t + π / 3) then -
	- (1) The current leads the emf by 60º
	- (2) The current lags the emf by 60º
	- (3) The emf leads the current by 60º
	- (4) The phase difference between the current and the emf is zero
- **Q.14** The direction of alternating current get changed in one cycle

Q.15 If the frequency of alternating potential is 50Hz then the direction of potential, changes in one second by -

(1) 50 times (2) 100 times (3) 200 times (4) 500 times

- **Q.16** The time period of of alternating current with frequency of one KHz one second will be $(1) 0.10$ $(2) 0.01$ (3) 1 \times 10⁻³ (4) 1 \times 10⁻²
- **Q.17** The value of alternating e.m.f. is $e = 500 \sin 100 \pi t$, then the frequency of this potential in Hz is - $(1) 25$ (2) 50 (3) 75 (4) 100
- **Q.18** The frequency of an alternating current is 50Hz, then the time to complete one cycle for current vector will be-

Q.19 In the above question, time taken by current to rise from zero to maximum is -

(1)
$$
\frac{1}{200}
$$
 sec
\n(2) $\frac{1}{100}$ sec
\n(3) $\frac{1}{50}$ sec
\n(4) $\frac{1}{400}$ sec

Q.20 In the equation for A.C. $I = I_0$ sin ωt , the current amplitude and frequency will respectively be -

(1) I₀,
$$
\frac{\omega}{2\pi}
$$
 (2) $\frac{I_0}{2}$, $\frac{\omega}{2\pi}$

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- (1) 2 $\frac{1}{\sqrt{2}}$ (i₁ + i₂) (2) 2 $\frac{1}{\sqrt{2}}$ $(i_1 + i_2)^2$ (3) 2 $\frac{1}{\sqrt{2}}$ $(i_1^2 + i_2^2)^{1/2}$ (4) 2 $\frac{1}{\sqrt{2}}$ $(i_1^2 + i_2^2)^{1/2}$
- **Q.32** The phase difference between the alternating current and voltage represented by the following equation $I = I_0$ sin ωt , $E = E_0 \cos(\omega t + \pi / 3)$, will be -

(1)
$$
\frac{\pi}{3}
$$

 (2) $\frac{4\pi}{3}$
 (3) $\frac{\pi}{2}$
 (4) $\frac{5\pi}{6}$

Q.33 The inductance of a resistance less coil is 0.5 Henry. In the coil the value of A.C. 0.2 Amp whose frequency is 50Hz. The reactance of circuit is -

 $Q.34$ The inductive reactance of a coil is 1000 Ω . If its self inductance and frequency both are increased two times then inductive reactance will be -

Q.35 In an L-C-R series circuit R = 10 Ω , X_L = 8 Ω and X_C = 6 Ω the total impedance of the circuit is -(1) 10.2Ω (2) 17.2Ω (3) 10Ω (4) None of the above

Q.36 In the given figure, the potential difference is shown on R, L and C. The e.m.f. of source in volt is -

Q.37 In an L.C.R series circuit R = 1Ω , X_L = 1000Ω and X_C = 1000Ω . A source of 100 m.volt is connected in the circuit the current in the circuit is - (1) 100 mAmp (2) 1 μ Amp $(3) 0.1 \mu$ Amp $(4) 10 \mu$ Amp

Q.38 Which of the following figure showing the phase relationship is correct phase diagram for an R–C circuit-

Q.39 A coil of inductance 0.1 H is connected to an alternating voltage generator of voltage E = 100 sin (100t) volt. The current flowing through the coil will be -

 (1) I = 10 $\sqrt{2}$ sin (100t) A (2) I = 10 $\sqrt{2}$ cos (100t) A $(3) I = -10 \sin (100t) A$ $(4) I = -10 \cos(100t)$ A

Q.40 The vector diagram of the current and voltage in a given circuit is shown in the figure. The components of the circuit will be -

Q.41 Figure shows the variation of voltage with time for an ac $I = I_0$ sin ωt flowing through a circuit -

- (1) Curve P is for R–L and Q for R–C circuit
- (2) Curve P is for R–C and Q for R–L circuit
- (3) Both are for R–C circuit
- (4) Both are for R–L circuit
- **Q.42** The power factor of the following circuit will be-

- **Q.43** In a circuit, the reactance of a coil is 20Ω . If the inductance of the coil is 50 mH then angular frequency of the current will be -
	- (1) 400 rad/sec (2) 1 rad/sec
	- (3) 2.5 rad/sec (4) 0.2 rad/sec
- **Q.44** If a capacitor is connected to two different A.C. generators then the value of capacitive reactance is -
	- (1) directly proportional to frequency
	- (2) inversely proportional to frequency
	- (3) independent of frequency
	- (4) inversely proportional to the square of frequency
- **Q.45** Alternating current lead the applied e.m.f. by $\pi/2$ when the circuit consists of -
	- (1) only resistance
	- (2) only capacitor
	- (3) only an inductance coil
	- (4) capacitor and resistance both
- **Q.46** The reactance of a capacitor is X_1 for frequency n_1 and X_2 for frequency n_2 then $X_1 : X_2$ is -
	- $(1) 1 : 1$ (2) $n_1 : n_2$ (3) $n_2 : n_1$ (4) $n_1^2 : n_2^2$
- **Q.47** A coil has reactance of 100 Ω when frequency is 50Hz. If the frequency becomes 150Hz, then the reactance will be -

Q.48 In pure inductive circuit, the curves between frequency f and inductive reactance $1/X_L$ is -

- **Q.49** In pure capacitive circuit if the frequency of A.C. is doubled, then the value of capacitive reactance will become -
	- (1) Two times (2) 1/2 times (3) No change (4) 1/4 times
- Q.50 In an A.C. circuit, a capacitor of 1uF value is connected to a source of frequency 1000 rad/sec. The value of capacitive reactance will be - (1) 10Ω (2) 100Ω
	- (3) 1000Ω (4) $10,000 \Omega$
- **Q.51** In an A.C. circuit capacitance of 5μ F has a reactance as $\frac{1}{1000}$ $\frac{1}{100}$ Ω . The frequency of A.C. in MHz will

Q.52 In an A.C. circuit $X_L = 300\Omega$, $X_C = 200\Omega$ and R = 100 Ω the impedance of circuit is -(1) 600Ω (2) 200Ω (3) 141Ω (4) None of the above

Q.53 A resistance of 50 Ω , an inductance of 20/ π Henry and a capacitor of 5/ π μ F are connected in series with an A.C. source of 230 volt and 50 Hz. The impedance of circuit is- (1) 5Ω (2) 50Ω (3) $5K\Omega$ (4) 500Ω

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- **Q.54** In an L–C–R series circuit R = $\sqrt{5}$ Ω , X_L = 9 Ω and X_C = 7 Ω . If applied voltage in the circuit is 50 volt then impedance of the circuit in ohm then impedance of the circuit in ohm will be - $(1) 2$ (2) 3
	- (3) 2 $\sqrt{5}$ (4) 3 $\sqrt{5}$
- **Q.55** The potential difference between the ends of a resistance R is V_R between the ends of capacitor is $V_c = 2V_R$ and between the ends of inductance is $V_L = 3V_R$, then the alternating potential of the source in terms of V_R will be -

(1) $\sqrt{2} V_R$ $(2) V_{R}$

(3) $V_R / \sqrt{2}$ $(4) 5V_R$

Q.56 In an A.C. circuit the impedance is $Z = 100\angle 30^\circ \Omega$, then the resistance of the circuit in ohm will be -

(1) 50 (2) 100 (3) 50 3 (4) 100 $\sqrt{3}$

Q.57 In an LCR circuit, the voltages across the components are V_L , V_C and V_R respectively. The voltage of source will be -

(1) $[V_R + V_L + V_C]$ (2) $[V_R^2 + V_L^2 + V_C^2]^{1/2}$ (3) $[V_R^2 + (V_L + V_C)^2]^{1/2}$ (4) $[V_R^2 + (V_L - V_C)^2]^{1/2}$

Q.58 In an electric circuit the applied alternating emf is given by E = 100 sin (314 t) volt, and current flowing I = sin (314t + π /3). Then the impedance of the circuit is (in ohm) -

 (1) 100 / $\sqrt{2}$ (2) 100

 $(3) 100 \sqrt{2}$ (4) None of the above

Q.59 The percentage increase in the impedance of an ac circuit, when its power factor changes form 0.866 to 0.5 is (Resistance constant)

Q.60 The impedance of the given circuit will be - 150Ω **~** ത്തത്ത 200Ω (1) 50 ohm (2) 150 ohm

(3) 200 ohm (4) 250 ohm

Q.61 The impedance of the given circuit will be -

Q.62 If $E_0 = 200$ volt, R = 25 ohm. L = 0.1 H and C = 10⁻⁵ F and the frequency is variable, then the current at $f = 0$ and $f = \infty$ will be respectively -

(3) 8 A, 8 A (4) 0 A, 0 A **Q.63** The impedance of the circuit given will be -

- (1) Zero (2) Infinite (3) 110 ohm (4) 90 ohm
- **Q.64** A coil of resistance R and inductance L is connected to a cell of emf E volt. The current flowing through the coil will be -
(1) F/R (2) F/I (1) F/R

(3)
$$
\frac{E}{\sqrt{L^2 + R^2}}
$$
 (4) $\frac{\sqrt{EL}}{\sqrt{L^2 + R^2}}$

Q.65 In a certain circuit E = 200 cos (314t) and I = sin (314t + $\pi/4$). Their vector representation is -

- **Q.66** In question (65) reactance X will be -(1) 70.7 ohm (2) 0.707 ohm (3) 100 ohm (4) 141 ohm
- **Q.67** In question (65) the power factor is - (1) 0.5 (2) 0.707 (3) 0.85 (4) 1.0

Q.68 The electric resonance is sharp in L-C-R circuit if in the circuit -

(1) R is greater (2) R is smaller

- (3) R = X_L or X_C (4) Does not depend on R
- **Q.69** In a series resonant L–C–R circuit, if L is increased by 25% and C is decreased by 20%, then the resonant frequency will -
	- (1) Increase by 10%
	- (2) Decrease by 10%
	- (3) Remain unchanged
	- (4) Increase by 2.5%

Q.70 If R = 100 Ω then the value of X and I in the given circuit will be

- **Q.71** In question (70) the value of inductance will be-(1) 0.12 H (2) 0.24 H $(3) 0.31 H$ (4) 0.43 H
- **Q.72** In an LCR. series circuit the resonating frequency can be decreased by -
	- (1) Decreasing the value of C
	- (2) Decreasing the value of L
	- (3) Decreasing both the values of L and C
	- (4) Increasing the value of C
- **Q.73** Which of the following statements is correct for L–C–R series combination in the condition of resonance -
	- (1) Resistance is zero
	- (2) Impedance is zero
	- (3) Reactance is zero
	- (4) Resistance, impedance and reactance all are zero
- **Q.74** In an LCR circuit, the resonating frequency is 500 kHz. If the value of L is increased two times and value of C is decreased $\frac{1}{8}$ $\frac{1}{6}$ times, then the new resonating frequency in kHz will be -(1) 250 (2) 500 (3) 1000 (4) 2000
- **Q.75** In resonating circuit value of inductance and capacitance is 0.1H and 200 μ F. For same resonating frequency if value of inductance is 100H then necessary value of capacitance in μ F will be -

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 (1) 4 (2) 0.2 (3) 2 (4) 0.3

- **Q.76** The inductance of the motor of a fan is 1.0 H. To run the fan at 50 Hz the capacitance of the capacitor that will cancel its inductive reactance, will be -
	- (1) 10 μ F (2) 40 μ F $(3) 0.4 \text{ }\mu\text{F}$ $(4) 0.04 \text{ }\mu\text{F}$
- **Q.77** In ac circuit at resonance -

(1) Impedance = R

(2) Impedance =
$$
\left(\omega L - \frac{1}{\omega C}\right)
$$

- (3) The voltages across L and C are in the same phase
- (4) The phase difference of current in C relative to source voltage is π
- **Q.78** An ac circuit resonates at a frequency of 10 kHz. If its frequency is increased to 11 kHz, then
	- (1) Impedance will increase by 1.1 times
	- (2) Impedance will remain unchanged
	- (3) Impedance will increase and become inductive
	- (4) Impedance will increase and become capacitive
- **Q.79** In an ac circuit 6 ohm resistor, an inductor of 4 ohm and a capacitor of 12 ohm are connected n series with an ac source of 100 volt (rms). The average power dissipated in the circuit will be - (1) 600 W (2) 500 W

Q.80 In an ac circuit emf and current are $E = 5 \cos \omega t$ volt and $I = 2 \sin \omega t$ ampere respectively. The average power dissipated in this circuit will be -

Q.81 The equations of alternating e.m.f. and current in an A.C. circuit are $E = 5 \cos \omega t$ volt and $I = 2$ sin ωt ampere respectively. The average power loss in this circuit will be -

Q.82 The series combination of resistance R and inductance L is connected to an alternating source of e.m.f. $e = 311 \sin(100 \pi t)$. If the value of wattless current is 0.5A and the impedance of the circuit is 311 Ω , the power factor will be -

(1)
$$
\frac{1}{2}
$$

\n(2) $\frac{1}{\sqrt{2}}$
\n(3) $\frac{1}{\sqrt{3}}$
\n(4) $\frac{1}{\sqrt{5}}$

Q.83 In an L–C–R series circuit the loss of power is in -

- (1) Only R (2) Only L
- (3) Only C (4) both L and C
- **Q.84** In an ac circuit the readings of an ammeter and a voltmeter are 10 A and 25 volt respectively, the power in the circuit will be -
	- (1) More than 250 W
	- (2) Always less than 250 W
	- (3) 250 W

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Q.85 A choke coil of 100 ohm and 1 H is connected to a generator of E = 200 sin (100t) volt. The average power dissipated will be -

- **Q.86** A choke coil of negligible resistance carries 5 mA current when it is operated at 220 V. The loss of power in the choke coil is -
	- (1) Zero (2) 11 W (3) 44 × 10³ W (4) 1.1 W
- **Q.87** The ratio of apparent power and average power in an A.C. circuit is equal to (1) Reciprocal of power factor
	- (2) Efficiency
	- (3) Power factor
	- (4) Form factor
- **Q.88** In an A.C. circuit, a resistance of 3 Ω , an inductance coil of 4 Ω and a condenser of 8 Ω are connected in series with an A.C. source of 50 volt (R.M.S.). The average power loss in the circuit will be -
	- (1) 600 watt (2) 500 watt (3) 400 watt (4) 300 watt
- **Q.89** In an A.C. circuit, $i = 5 \sin(100t \frac{\pi}{2})$ $\frac{\pi}{2}$) ampere an A,V, V = 200 sin (100 t) volt. The power loss in the circuit will be - (1) 20 volt (2) 40 volt (3) 1000 watt (4) 0 watt
- **Q.90** When N identical bulbs are connected in parallel, total power consumption is P, what would be the power consumption when they connected in series- (1) P (2) PN (3) P/N (4) P/N²
- **Q.91** Two bulbs of 500 watt and 300 watt work on 200 volt r.m.s. the ratio of their resistances will be- (1) 25 : 9 (2) 3 : 5 (3) 9 : 25 $-(4)$ 5 : 9
- **Q.92** An air core coil and an electric bulb are connected in series with an A.C. source. If an iron rod is put in the coil, then the intensity of bulb's will- (1) Be same (2) Increase
	- (3) Decrease (4) Decrease, increase
- **Q.93** If a bulb and a coil are connected in series with D.C. source and a iron core put in the coil then the glowing of bulb -
	- (1) Decreases (2) Increases
		- (3) No change (4) Zero
- **Q.94** Three bulbs of 40, 60 and 100 watt are connected in series with the source of 200 volt. Then which of the bulb will be glowing the most -
	- (1) 100 watt
	- (2) 60 watt
	- (3) 40 watt
	- (4) All are glowing equally
- **Q.95** If two bulbs each of 220V, 30 watt are connected in series, then we get electric power as (1) 60 watt (2) 15 watt

(3) 6 watt (4) 30 watt

Q.96 Two electric bulbs of 100 watt (220 volt) are connected in series and these are connected with other bulb of 100W (220V) in parallel then total power in watt will be -

- **Q.97** The A.C. meters are based on the principle of
	- (1) Heating effect
	- (2) magnetic effect
	- (3) Chemical effect
	- (4) Electromagnetic effect

Q.98 The correctly marked ammeter for A.C. current is shown in

- **Q.99** Alternating current can not be measured by direct current meters, because
	- (1) alternating current can not pass through an ammeter
	- (2) the average value of current for complete cycle is zero
	- (3) some amount of alternating current is destroyed in the ammeter
	- (4) None of these
- **Q.100** The A.C. meters measure its
	- (1) root mean square value
	- (2) peak value
	- (3) square mean value
	- (4) None of the above

IMPORTANT PRACTICE QUESTION SERIES FOR IIT-JEE EXAM – 2

-
- **Q.1** The self inductance of a choke coil is 10mH. When it is connected with a 10V D.C. source, then the loss of power is 20 watt. When it is connected with 10 volt A.C. source loss of power is 10 watt. The frequency of A.C. source will be -
	- (1) 50Hz (2) 60Hz (3) 80Hz (4) 100Hz
- **Q.2** We have two cables of copper of same length. In one, only one wire of cross–section area A and in second ten wires each of cross–section area A/10 are present. When A.C. and D.C. flow in it. Choose the correct cable for better efficiency -
	- (1) Only one wire for D.C. and the other for A.C
	- (2) Only one wire for A.C. and the other for D.C.

- (3) Any wire for D.C. but only multy–wire cable for A.C.
- (4) Only one wire for D.C. and only multy–wire packet for A.C.
- **Q.3** In a series LCR circuit L = 1H, C = 6.25 μ F and R = 1 ohm. Its quality factor is -(1) 400 (2) 200 (3) 125 (4) 25
- **Q.4** A bulb of rated values 60 V and 10 W is connected in series with a source of 100 V and 50 Hz. The coefficient of self induction of a coil to be connected in series for its operation will be - (1) 1.53 H (2) 2.15 H (3) 3.27 H (4) 3.89 H
- **Q.5** Two identical bulbs B_1 and B_2 are connected to an ac source. B is connected in series with a coil of 100 mH and B_2 with a capacitor of 10 μ F as shown in the figure. The brightness of B_1 and B_2 will be-

- (1) Same in both
- (2) More in B_1
- (3) Depending on the frequency of the source
- (4) More in $B₂$
- **Q.6** An L–C–R series circuit with a resistance of 100 ohm is connected to an ac source of 200 V (rms) and angular frequency 300 rad/s. When only the capacitor is removed. the current lags behind the voltage by 60º. When only the inductor is removed , the current leads with the voltage by 60º. The average power dissipated is-
	- (1) 50W (2) 100 W (3) 200 W (4) 400 W
- **Q.7** A coil when connected to a dc source of 12 V, carries a current of 4 A. If this coil is connected to an ac source of 12 V and 50 rad/s, then it carries a current of 2.4 A. The inductance of the coil is - (1) 48 H (2) 4 H (3) 12.5 H (4) 8×10^{-2} H
- **Q.8** Waves of wavelength 300 m are transmitted from a broadcasting station. If a capacitor f 2.4 µF is used in a resonant circuit for these waves, then the inductance of coil used will be- (1) 10⁻⁶ H (2) 1.056 × 10⁻⁸ H (3) 10.56 \times 10⁻⁸ H (4) 105.6 \times 10⁻⁸ H
- **Q.9** A generator of 100 V (rms) is connected in an ac circuit and 1 A (rms) current is flowing in the circuit. If the phase difference between the voltage and the current is $\pi/3$. then the average power consumption and the power factor of the circuit will be -

Q.10 When a current of 0.5 A (rms) is passed through a coil, its reactance and power loss are found to be 25 ohm and 16 W. The impedance of the coil is -

(1) 50 ohm (2) 68.7 ohm (3) 76.4 ohm (4) 92.3 ohm

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Q.11 In the adjoining A.C. circuit the voltmeter whose reading will be zero at resonance is -

- (1) V_1 $(2) V₂$
- $(3) V₃$ (4) V_4
- **Q.12** In the above problem, the two voltmeters whose readings are equal, will be -(1) V_4 and V_1 (2) V_1 and V_3 (3) V_4 and V_5 (4) V_1 and V_2
- **Q.13** In Q.11, if $\omega L / R = 10$ and $V_3 = 100$ volt then reading of V_2 will be -(1) 10 volt (2) 100 volt (3) 1000 volt (4) uncertain
- **Q.14** 2.5/ π µF capacitor and a 3000–ohm resistance are joined in series to an a.c. source of 200 volt and 50 sec⁻¹ frequency. The power factor of the circuit and the power dissipated in it will respectively - (1) 0.6, 0.06W (2) 0.06, 0.6W (3) 0.6, 4.8W (4) 4.8, 0.6W
- **Q.15** The current through 'a' wire changes with time according to the equation $I = \sqrt{t}$. The correct value of the rms current within the time interval $t = 2$ to $t = 4s$ will be -

 $(1)\sqrt{3}$ $(2) 3 A$ $(3) 3 \sqrt{3}$ (4) None of the above

Q.16 The time required for a 50 Hz alternating current to increase from zero to 70.7% of its peak value is -

- **Q.17** Figure 92 shows an AC generator connected to a "block box" through a pair of terminals. The box contains possible R,L, C or their combination, whose elements and arrangements are not known to us. Measurements outside the box reveals that
	- $e = 75 \sin{(\omega t)}$ volt,

 $i = 1.5 \sin (\omega t + 45^{\circ})$ amp

then, the wrong statement is -

- (1) There must be a capacitor in the box
- (2) There must be an inductor in the box
- (3) There must be a resistance in the box
- (4) The power factor is 0.707
- **Q.18** In ac circuit contains a pure capacitor, across which an ac emf e = 100 sin (1000t), volt is applied. If the peak value of the current is 200 mA, then the value of the capacitor is - (1) 2μ F (2) 20μ F

(1) must be zero (2) may be zero

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(3) is never zero

(4) is
$$
\frac{20}{\sqrt{2}}
$$
 volt

Q.27 An AC ammeter is used to measure current in a circuit. When a given direct current passes through the circuit, the AC ammeter reads 3A. When another alternating current passes through the circuit the AC ammeter reads 4 A, then reading of this ammeter if DC and AC flow through the circuit simultaneously is-

(1) 3 A (2) 4 A (3) 7 A (4) 5 A

Q.28 An inductor (L) and resistance (R) are connected in series with an AC source. The phase difference between voltage (V) and current (i) is 45°. Now a capacitor (3) is connected in series with L-R, If the phase difference between V and i remain same, then capacitive reactance and impedance of L-C-R circuit will be-

Q.29 In a series LCR circuit the voltage across the resistance, capacitance and inductance is 10 V each. If the capacitor is removed, the voltage across the inductance will be-

(1) 10 V (2)
$$
10\sqrt{2}V
$$
 (3) $\frac{10}{\sqrt{2}}V$ (4) 20 V

Q.30 An alternating emf 100 cos 100 t volt is connected in series to a resistance of 10 Ω and inductance 100 mH, what is the phase difference between the current in the circuit and the emf-

(1)
$$
\frac{\pi}{4}
$$
 (2) zero (3) π (4) $\frac{\pi}{2}$

Q.31 A coil having an inductance of π 1 Henry is connected in series with a resistance of 300 Ω . If 20 V from a 200 cycle/s source are impressed across the combination. The power factor of the circuit will be-

(1)
$$
\frac{2}{5}
$$
 (2) $\frac{3}{5}$ (3) $\frac{4}{5}$ (4) $\frac{2}{3}$

- **Q.32** In an AC circuit, a resistance of R ohm is connected in series with an inductance L. If phase angle between voltage and current be 45°, the value of inductive reactance will be-
	- (1) R/4
	- (2) R/2
	- (3) R
	- (4) Cannot be found with the given data
- **Q.33** In LCR series AC circuit, the phase angle between current and voltage is-

(1) any angle between 0 and $\pm \pi/2$

- (2) $\pi / 2$
- (3) π

(4) any angle between 0 and π

Q.34 A coil has an inductance of 0.7 H and is joined in series with a resistance of 220 Ω . When an alternating e.m.f. of 220 V at 50 cps is applied to it, then the wattless component of the current in the circuit is-

Q.35 A direct current of 2 A and an alternating current having a maximum value of 2 A flow through two identical resistances. The ratio of heat produced in the two resistances will be- $(1) 1 : 1$ $(2) 1 : 2$ $(3) 2 : 1$ $(4) 4 : 1$

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- **Q.36** An alternating voltage is connected in series with a resistance R and an inductance L. If the potential drop across the resistance is 200 volt and across the inductance is 150 volt, the applied voltage is-
	- (1) 350 volt (2) 250 volt (3) 500 volt (4) 300 volt
- **Q.37** An AC circuit using an inductor and a capacitor in series has a maximum current. If L = 0.5 H and C $= 8 \mu$ F, then the angular frequency of input AC voltage will be -
	- (1) 500 (2) 5×10^5
	- (3) 4000 (4) 5000
- **Q.38** A resistor and an inductor are connected to an AC supply of 120 volt and 50 Hz. The current in the circuit is 3 ampere. If the power consumed in the circuit is 108 watt, then the resistance in the circuit is-

- $(3) \sqrt{52 \times 28}$ ohm (4) 360 ohm
- **Q.39** In an AC circuit, the current lags behind the voltage by $\pi/3$. The components of the circuit are-(1) R and L (2) L and C
	- (3) R and C (4) only R
- **Q.40** A 10 ohm resistance, 5 mH coil and 10 µF capacitor are joined in series. When a suitable frequency alternating current source is joined to the combination the circuit resonates. If the resistance is halved, the resonance frequency-
	- (1) is halved (2) is doubled
	- (3) remains unchanged (4) is quadrupled
- **Q.41** A conducting wire is stretched between the poles of a magnet. There is a strong uniform magnetic field in the region between the poles. If an alternating current

is passed through the wire AB, the wire will-

(1) remain stationary

- (2) be pulled towards north pole
- (3) be pulled towards south pole
- (4) vibrate with a frequency $\omega/2\pi$
- **Q.42** In an LR circuit, the inductive reactance is equal to resistance R of the circuit. An e.m.f. $E = E_0 \cos \omega t$ is applied to the circuit. The power consumed in the circuit is-

- **Q.43** The voltage of an AC supply varies with time (t) as $V = 120 \sin 100 \pi t \cos 100 \pi t$. The maximum voltage and frequency respectively are -
	- (1) 60 volt, 100 Hz
	- (2) 2 $\frac{120}{\sqrt{2}}$ volt, 100 Hz
	- (3) 120 volt, 100 Hz
	- (4) 60 volt, 200 Hz

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IMPORTANT PRACTICE QUESTION SERIES FOR IIT-JEE EXAM – 3

Q.1 The value of quality factor is-

Q.2 A capacitor of capacity C and reactance X if capacitance and frequency become double then reactance will be-

(1) 4X (2)
$$
\frac{X}{2}
$$
 (3) $\frac{X}{4}$ (4) 2X

Q.3 For a series LCR circuit the power loss at resonance is-

$$
(1) \frac{V^2}{\left[\omega L - \frac{1}{\omega C}\right]}
$$
\n
$$
(2) l^2 L \omega
$$
\n
$$
(3) l^2 R \qquad (4) \frac{V^2}{C\omega}
$$

Q.4 In a circuit L, C and R are connected in series with an alternating voltage source of frequency f. The current leads the voltage by 45º. The value of C is-

(1)
$$
\frac{1}{2\pi f(2\pi fL - R)}
$$
 (2) $\frac{1}{2\pi f(2\pi fL + R)}$
(3) $\frac{1}{\pi f(2\pi fL - R)}$ (4) $\frac{1}{\pi f(2\pi fL + R)}$

Q.5 A transistor-oscillator using a resonant circuit with an inductor L (of negligible resistance) and a capacitor C in series produce oscillations of frequency f. If L is doubled and C is changed to 4C, then frequency will be-

(1)
$$
\frac{f}{4}
$$
 (2) 8f (3) $\frac{f}{2\sqrt{2}}$ (4) $\frac{f}{2}$

- **Q.6** A coil of inductive reactance 31 Ω has a resistance of 8 Ω . It is placed in series with a condenser of capacitative reactance 25 Ω . The combination is connected to an a.c. source of 110 volt. The power factor of the circuit is- (1) 0.56 (2) 0.64 (3) 0.80 (4) 0.33
- **Q.7** What is the value of inductance L for which the current is a maximum in a series LCR circuit with C $= 10 \mu$ F and $\omega = 1000 \text{ s}^{-1}$?

(1) 10 mH

(2) 100 mH

 $(3) 1 mH$

- (4) cannot be calculated unless R is known
- **Q.8** In an a.c. circuit the e.m.f. (e) and the current (i) at any instant are given respectively by-

 $e = E_0 \sin \omega t$ $i = I_0 \sin(\omega t - \phi)$

The average power in the circuit over one cycle of a.c. is-

(1)
$$
\frac{E_0 I_0}{2} \cos \phi
$$
 (2) $E_0 I_0$
(3) $\frac{E_0 I_0}{2}$ (4) $\frac{E_0 I_0}{2} \sin \phi$

Q.9 The reactance of an inductance of 0.01 H for 50 Hz A.C. is- (1) 6.28 Ω (2) 3.14 Ω

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(3) 1.57 Ω (4) 0.84 Ω

Q.10 In an A.C. circuit containing only capacitance, the current-

(1) leads the voltage by 90º

- (2) leads the voltage by 180º
- (3) lags the voltage by 90º
- (4) remains in phase with the voltage
- **Q.11** A choke coil should have-
	- (1) high resistance and low inductance
	- (2) high resistance and high inductance
	- (3) low resistance and high inductance
	- (4) low resistance and low inductance
- **Q.12** The impedance of a circuit, when a resistance R and an inductor of inductance L are connected in series in an A.C. circuit of frequency (f) is-

(1)
$$
\sqrt{R + 4\pi fL^2}
$$

\n(2) $\sqrt{R + 4\pi^2 f^2 L^2}$
\n(3) $\sqrt{R^2 + 4\pi^2 f^2 L^2}$
\n(4) $\sqrt{R^2 + 2\pi^2 f^2 L^2}$

- **Q.13** The coil of choke in a circuit- (1) increases the current (2) decreases the current (3) has high resistance to d.c. circuit
	- (4) does not change the current
- **Q.14** A capacitor of capacitance 2μ F is connected in the tank circuit of an oscillator oscillating with a frequency of 1 kHz. If the current flowing in the circuit is 2mA, the voltage across the capacitor will be-

(1) 0.16 V (2) 0.32 V (3) 79.5 V (4) 159 V

Q.15 A 50 Hz a.c. source of 20 volts is connected across R and C as shown in figure below. The voltage across R is 12 volts. The voltage across C is-

- (1) 8 V
- (2) 16 V
- (3) 10 V
- (4) Not possible to determine unless values of R and C are given
- **Q.16** Power dissipated in an LCR series circuit connected to an a.c. source of emf ε is-

$$
(1) \varepsilon^{2} R / \sqrt{R^{2} + \left(L\omega - \frac{1}{C\omega}\right)^{2}}
$$
\n
$$
(2) \varepsilon^{2} R / \left[R^{2} + \left(L\omega - \frac{1}{C\omega}\right)^{2}\right]
$$
\n
$$
(3) \varepsilon^{2} \sqrt{R^{2} + \left(L\omega - \frac{1}{C\omega}\right)^{2}} / R
$$
\n
$$
\varepsilon^{2} \left[R^{2} + \left(L\omega - \frac{1}{C\omega}\right)^{2}\right]
$$
\n
$$
(4) \frac{\varepsilon^{2} \left[R^{2} + \left(L\omega - \frac{1}{C\omega}\right)^{2}\right]}{R}
$$

Q.17 In the given circuit the reading of voltmeter V_1 and V_2 are 300 volts each. The reading of the voltmeter V_3 and ammeter A are respectively –

(1) 150 V, 2.2 A (2) 220 V, 2.2 A (3) 220 V, 2.0 A (4) 100 V, 2.0 A

Q.18 A 220 volt input is supplied to a transformer. The output circuit draws a current of 2.0 ampere at 440 volts. If the efficiency of the transformer is 80%, the current drawn by the primary windings of the transformer is –

- **Q.19** In an ac circuit an alternating voltage $e = 200\sqrt{2}$ sin 100 t volts is connected to a capacitor of capacity 1 µF. The r.m.s. value of the current in the circuit is : (1) 20 mA (2) 10 mA
	- (3) 100 mA (4) 200 mA
- **Q.20** An ac voltage is applied to a resistance R and an inductor L in series. If R and the inductive reactance are both equal to 3 Ω , the phase difference between the applied voltage and the current in the circuit is :

(1) zero (2) $\pi/6$ (3) $\pi/4$ (4) $\pi/2$

Q.21 The r.m.s. value of potential difference V shown in the figure is :

Q.22 A coil has resistance 30 ohm and inductive reactance 20 Ohm at 50 Hz frequency. If an ac source, of 200 volt, 100 Hz, is connected across the coil, the current in the coil will be (1) 2.0 A (2) 4.0 A

 $(3) 8.0 A$

13 $rac{20}{\sqrt{2}}$ A

г

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(2) Lagging, potential by $\pi/2$

(3) in same phase with potential

(4) With a phase difference of π with potential

- **Q.13** In an A.C. circuit capacitance of 5 μ F has a reactance as 1000 Ω . The frequency of A.C. will be-
	- (1) $\frac{100}{\pi}$ $\frac{1000}{\pi}$ cycle/s (2) $\frac{10}{\pi}$ $\frac{100}{2}$ cycle/s
	- (3) 200 cycle/s (4) 5000 cycle/s
- **Q.14** The impedance of L-R circuit is shown by- (1) LR (2) L/R (3) $\sqrt{L^2 \omega^2 + R^2}$ (4) $\sqrt{R^2 \omega^2 + L^2}$
- **Q.15** Alternating current is flowing in inductance L and resistance R. The frequency of source is $\omega/2\pi$. Which of the following statement is correct-
	- (1) For low frequency the limiting value of impedance is L
	- (2) For high frequency the limiting value of impedance is ωL
	- (3) For high frequency the limiting value of impedance is R
	- (4) For low frequency the limiting value of impedance is ω .
- **Q.16** In an A.C. circuit inductance, capacitance and resistance are connected. If the effective voltage across inductance is V_L , across capacitance is V_C and across resistance is V_R , then the total effective value of voltage is-

(1)
$$
V_R + V_L + V_C
$$

\n(2) $V_R + V_L - V_C$
\n(3) $\sqrt{V_R^2 + (V_L - V_C)^2}$
\n(4) $\sqrt{V_R^2 - (V_L - V_C)^2}$

- **Q.17** In an L-C-R series resonating circuit the relation between X_L and X_C is-
	- (1) $X_L/X_C = 1$ (2) $X_L/X_C > 1$ (3) $X_L/X_C < 1$ (4) $X_L/X_C = -1$
- **Q.18** Two different AC circuits have same current. One is containing only inductance while the other contains only capacitance. If the frequency of applied emf is increased then the current will change as-
	- (1) increase in first and decrease in second
	- (2) decrease in both
	- (3) increase in both
	- (4) decrease in first and increase in second
- **Q.19** Which one of the following has not the same unit-

1

R L

$$
(1) \sqrt{LC}
$$
\n
$$
(2) \frac{1}{\sqrt{LC}}
$$
\n
$$
(3) RC
$$
\n
$$
(4) \frac{L}{R}
$$

Q.20 If the output of an A.C. generator is E = 170sin377t, then the frequency will be-

- (1) 50 Hz (2) 110 Hz
- (3) 60 Hz (4) 230 Hz
- **Q.21** The r.m.s value of alternating current is-
	- (1) Double of peak value
	- (2) Half of peak value
- (3) 2 $\frac{1}{\sqrt{2}}$ times of peak value (4) Equal to peak value
- **Q.22** The r.m.s. value of current for a variable current $i = i_1 \cos \omega t + i_2 \sin \omega t$ -

(1)
$$
\frac{1}{\sqrt{2}} (i_1 + i_2)
$$
 (2) $\frac{1}{\sqrt{2}} (i_1 + i_2)^2$
(3) $\frac{1}{\sqrt{2}} (i_1^2 + i_2^2)^{1/2}$ (4) $\frac{1}{2} (i_1^2 + i_2^2)^{1/2}$

- **Q.23** The inductance of a coil is 0.70 henry. An A.C. source of 120 volt is connected parallel with it. If the frequency of A.C. is 60 Hz, then the current which is flowing in inductance, will be- (1) 4.55 amp (2) 0.355 amp (3) 0.455 amp (4) 3.55 amp
- **Q.24** A capacitor of capacity C is connected in A.C. circuit. The applied emf is $V = V_0$ sinot, then the current is-

(1)
$$
1 = \frac{V_0}{\omega L} \sin \omega t
$$

\n(2) $1 = \frac{V_0}{\omega L} \sin(\omega t + \pi/2)$
\n(3) $1 = V_0 \omega C \sin(\omega t + \pi/2)$

(4) $I = V_0 \omega \text{Csin}(\omega t + \pi/2)$

- **Q.25** In an A.C. circuit, a capacitor of 1 µF value is connected to a source of frequency 1000 rad/s. The value of capacitive reactance will be- (1) 10 Ω (2) 100 Ω (3) 1000Ω (4) $10,000 \Omega$
- **Q.26** In an A.C. circuit resistance and inductance are connected in series. The potential and current in inductance is-

(1)
$$
V_0 \sin \omega t
$$
, $\frac{V_0}{\omega L} \sin \omega t$

(2) V_osin
$$
\omega
$$
, $\frac{V_0}{\omega L}$ sin($\omega t + \pi/2$)

(3)
$$
V_0 \sin(\omega t + \pi/2)
$$
, $\frac{V_0}{\omega L} \sin \omega t$
(4) $V_0 \sin(\omega t + \pi/2)$, $\frac{V_0}{\omega L} \sin(\omega t - \pi/2)$

- **Q.27** Which of the following statements is correct, for an LCR series combination having the resonating condition as-
	- (1) the current is minimum
	- (2) the phase difference between the current and e.m.f. is $\pi/2$
	- (3) the tempedance is equal to R
	- (4) the value of power factor is minimum
- **Q.28** The current I = $I_0\sin(\omega t \pi/2)$ is flowing in a variable current circuit. The potential $E = E_0$ sin ωt is applied to the circuit. The loss of power will be-

 $(1) P = E_0 I_0 / \sqrt{2}$ (2) $P = E_0 I_0 / 2$ $(3) P = E1/\sqrt{2}$ $(4) P = zero$

- **Q.29** Power factor of a best choke coil is- (1) Near about zero (2) Zero (3) Near about one (4) One
- **Q.30** The peak value of alternating potential is E_0 then r.m.s. value of the same will be-
	- $(1) E_0/2$ (2) $\sqrt{E_0}$ (3) $E_0 / \sqrt{2}$ (4) $E_0 \sqrt{2}$
- **Q.31** In an inductive circuit the equation of A.C., is $i = i_0$ sin ωt then-(1) $E = E_0 \sin(\omega t + \pi/2)$ (2) $E = E_0 \sin(\omega t - \pi/2)$ (3) $E = E_0 \sin \omega t$ (4) None of the above
- **Q.32** In an A.C. circuit, the reactive reactance X_1 (1) $2\pi f$ (2) $1/(2\pi f)$ (3) πf (2) (4) $2/\pi f$ (4)
- **Q.33** A coil has reactance of 100 Ω . When frequency is 50 Hz. If the frequency becomes 150 Hz, then the reactance will be- (1) 100Ω (2) 300Ω (3) 450Ω (4) 600Ω
- **Q.34** If a choke of negligible resistance works on 220V source and 5mA current is flowing through it, then the loss of power in choke coil is- (1) zero (2) 11 watt (3) 44×10^3 watt (4) 1.1 watt
- **Q.35** Correct expression for A.C.

 $(1) \tan \theta =$ - R C $\omega L - \frac{1}{\omega}$ $(2) sin θ =$ R C 1 L ω $\omega L (3) \cos\theta =$ - R C $\omega L - \frac{1}{\omega}$ (4) None of these

Q.36 In the given figure, the potential difference is shown on R, L and C. The e.m.f. of source in volt is-

Q.37 In an alternating current circuit L = 0.5 H and C = 8 μ F. For maximum value of current in the circuit the angular frequency will be-

Q.38 A circuit with e.m.f. E = 200sin ω t and I = sin ω t, contains a capacitance and inductance, then the value of power factor will be-

 $(1) 0$ $(2) 1$ $(3) 0.6$ $(4) 0.3$

- **Q.39** In a resistance of 25 Ω A.C. is passed to produce heat of the rate of 250 watt. The value of current in the resistance will be-
	- $(1) 0.316 A$ $(2) 1 A$ (3) 3.16 A (4) 10 A
- **Q.40** A choke coil has-
	- (1) Low resistance and high inductance
	- (2) High resistance and high inductance
	- (3) Low resistance and low inductance

- (4) High resistance and low inductance
- **Q.41** In an LCR circuit C = 25 µF, L = 0.1H, R = 25 Ω , if E = 310 sin 314 t volts in the generator voltage which is connected in the circuit then the value of current in the circuit is- (1) i = 5.4sin(314t – ϕ) (2) i = 3.1 sin(314t + ϕ) (3) i = 3.1sin(314t – ϕ) (4) i = 3.46 sin(314t + ϕ)
- **Q.42** In an LCR circuit C=25 µF, L = 0.1H, R = 25Ω , if E = 310 sin 314 t volts is the generator voltage which is connected in the circuit then, how much inductance should be connected so that impedance is minimum-

- **Q.43** 5 cm long 10 Ω resistance and 5 mH inductance of a solenoid, is connected with 10 volt battery. The value of current which flows in stable condition of solenoid in ampere is- (1) 5 (2) 1 (3) 2 (4) Zero
- **Q.44** The value of current at half power points is-

Q.45 The self inductance of a choke coil is 10 mH. When it is connected with a 10V D.C. source, then the loss of power is 20 watt. When it is connected with 10 volt A.C. source loss of power is 10 watt. The frequency of A.C. source will be-

Q.46 The inductance of a choke coil is 0.2 henry and its resistance is 0.50 ohm. If a current of 2.0 amp (rms value) and frequency 50 hertz be passed through it. What will be the potential difference across its ends-

(1) 125.6 volt (2) 250.1 volt (3) 62.5 volt (4) none of these

Q.47 An alternating voltage $E = 200\sqrt{2} \sin(100t)$ volt is connected to a 1 μ F capacitor through an A.C. ammeter. The reading of ammeter is-

- **Q.48** In an A.C. circuit V and I are given by $V = 100 \sin(100t)$ volts $I = 100 \sin(100t + \pi/3)$ mA The power dissipated in the circuit is- (1) 10⁴ watt (2) 10 watt
	- (3) 2.5 watt (4) 5.0 watt

Q.49 An alternating e.m.f. of frequency $\overline{}$ $\overline{}$ $\bigg)$ \backslash l I $\overline{}$ ſ π $|v| =$ $2\pi\sqrt{LC}$ 1 is applied to a series LCR circuit. For this

frequency of the applied e.m.f.-

- (1) The circuit is at resonance and its impedance is made up only of a reactive part
- (2) The current in the circuit is out of phase with the applied e.m.f. and the voltage across R equals this applied e.m.f.
- (3) The sum of the p.d's across the inductance and capacitance equals the applied e.m.f. which is 180º ahead of phase of the current in the circuit
- (4) The quality factor of the circuit is $\omega L/R$ or $1/\omega CR$ and this a measure of the voltage magnification (produced by the circuit at resonance of the circuit

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- **Q.50** A bulb and a capacitor are connected in series to a source of alternating current. If its frequency is increased, while keeping the voltage of the source constant, then-
	- (1) Bulb will give more intense light
	- (2) Bulb will give less intense light
	- (3) Bulb will give light of same intensity as before
	- (4) Bulb will stop radiating light

Q.51 The inductance of the oscillatory circuit of a radio station is 10 milli henry and its capacitance is 0.25 µF. Taking the effect of the resistance negligible, wavelength of the broadcasted waves will be (velocity of light = 3.0×10^8 m/s, π = 3.14)

(1) 9.42×10^4 m (2) 18.8×10^4 m

- (3) 4.5×10^4 m (4) none of these
- **Q.52** A coil has an inductance of 0.7 henry and is joined in series with a resistance of 220 Ω . When the alternating emf of 220 V at 50 Hz is applied to it then the phase through which current lags behind the applied emf and the wattless component of current in the circuit will be respectively-

(1) 30º, 1 A (2) 45º, 0.5 A $(3) 60^{\circ}$, 1.5 A (4) none of these

Q.53 If value of R is changed, then-

- (1) Voltage across L remains same
- (2) Voltage across C remains same
- (3) Voltage across LC combination remains same
- (4) Voltage across LC combination changes
- **Q.54** When 100 V D.C. is applied across a coil a current of 1A flows through it. When 100V A.C. of 50 Hz is applied to the same coil only 0.5A flows. The inductance of the coil is- (1) 0.55 H (2) 55 mH
	- (3) 0.55 mH (4) 5.5 mH
- **Q.55** In the circuit shown in the figure, the A.C. source gives a voltage V = 20cos(2000t) volt neglecting source resistance, the voltmeter and ammeter readings will be-

 $\frac{1}{2}$ henry and 50 Hz-

(3) 0 V, 0.47 A (4) 1.68 V, 0.47 A

 $(1) 0 V, 1.4 A$ (2) 5.6 V, 1.4 A

Q.56 The inductive reactance of an inductive coil with $\frac{1}{\pi}$

- **Q.57** In an alternating circuit applied voltage and flowing current are $E = E_0 sin \omega t$ and $I = I_0 \sin(\omega t + \pi/2)$ respectively. Then the power consumed in the circuit will be-
	- (1) Zero (2) $E_0I_0/2$ (3) $E_0 I_0 / \sqrt{2}$ (4) $E_0I_0/4$
- **Q.58** In the L-R circuit R = 10 Ω and L = 2H. If 120V, 60Hz alternating voltage is applied then that the flowing current in this circuit will be- (1) 0.32 A (2) 0.16 A

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(3) 0.48 A (4) 0.80 A

Q.59 The relation between an A.C. voltage source and time in SI units is- V = $120\sin(100\pi t)\cos(100\pi t)$ volt value of peak voltage and frequency will be respectively-

(1) 120 volt and 100 Hz

- (2) 2 $\frac{120}{\sqrt{2}}$ volt and 100 Hz
- (3) 60 volt and 200 Hz
- (4) 60 volt and 100 Hz

Q.60 In which of the following case power factor will be negligible-

- (1) Inductance and resistance both high
- (2) Inductance and resistance both low
- (3) Low resistance and high inductance

(4) High resistance and low inductance

- **Q.61** An inductance of 0.4 Henry and a resistance of 100 ohm are connected to a A.C. voltage source of 220 V and 50 Hz. Then find out the phase difference between the voltage and current flowing in the circuit-
	- (1) tan⁻¹(2.25 π) (2.25π) (2) tan⁻¹(0.4 π) (3) tan⁻¹(1.5 π) (1.5π) (4) tan⁻¹(0.5 π)
- **Q.62** Choke coil-

(1) Decreases current in A.C. (2) Increases current in A.C. (3) Decreases current in D.C.

- (4) Increases current in D.C.
- **Q.63** In a circuit 20 Ω resistance and 0.4 H inductance are connected with a source of 220 volt of frequency 50 Hz, then the value of ϕ will be-

Q.64 If V = 100sin100t volt, and I = 100sin(100t + $\frac{\pi}{6}$ $\frac{\pi}{6}$)A, then find the watt less power in watt-

- **Q.65** If an A.C. main supply is given to be 220 V. What would be the average e.m.f. during a positive half cycle-
	- (1) 198 V (2) 386 V (3) 256 V (4) None of these
- **Q.66** An inductor and a resistor in series are connected to an A.C. supply of variable frequency. As the frequency of the source is increased, the phase angle between current and the potential difference across source will be-

- (1) First increase and then decrease
- (2) First decrease and then increase
- (3) Go on decreasing
- (4) Go on increasing

Q.67 An A.C. supply gives 30 V r.m.s. which passes through a 10 Ω resistance. The power dissipated in it is-

Q.68 The diagram shows a capacitor C and a resistor R connected in series to an AC source, V_1 and V_2 are voltmeters and A is an ammeter. Consider now the following statements-

(I) Readings in A and V_2 are always in phase

(II) Reading in V_1 is ahead with reading in V_2

(III) Readings in A and V_1 are always in phase

Which of these statements are is correct-

(1) I only (2) II only (3) I and II only (4) II and III only

Q.69 In a series LCR circuit voltage across resister, inductor and capacitor are 1 V, 3 V and 2 V respectively. At the instant t when the source voltage is given by $V = V_0 \cos \omega t$, the current in the circuit will be-

(1)
$$
1 = I_0 \cos \left(\omega t + \frac{\pi}{4}\right)
$$
 (2) $1 = I_0 \cos \left(\omega t - \frac{\pi}{4}\right)$
(3) $1 = I_0 \cos \left(\omega t + \frac{\pi}{3}\right)$ (4) $1 = I_0 \cos \left(\omega t - \frac{\pi}{3}\right)$

- **Q.70** Phase difference between V and I at resonance is- (1) 0 (2) $2\pi/3$ (3) $\pi/3$ (4) None of these
- **Q.71** A capacitor of capacitance 100 μ F and a resistance of 100 Ω is connected in series with AC supply of 220V, 50 Hz. The current leads the voltage by

(1)
$$
\tan^{-1}\left(\frac{1}{2\pi}\right)
$$
 (2) $\tan^{-1}\left(\frac{1}{\pi}\right)$
(3) $\tan^{-1}\left(\frac{2}{\pi}\right)$ (4) $\tan^{-1}\left(\frac{4}{\pi}\right)$

Q.72 In an AC circuit decrease in impedance with increase in frequency is indicates that circuit has/have-

(1) only resistance

- (2) resistance and inductance
- (3) resistance and capacitance
- (4) resistance, capacitance and inductance
- **Q.73** For given circuit the power factor is-

 $(1) 0$ $(2) 1/2$ $(3) 1/\sqrt{2}$ (4) None

Q.74 If the current through an inductor of inductance L is given by $I = I_0$ sinot, then the voltage across inductor will be-

(1) $I_0 \omega L \sin(\omega t - \pi/2)$ (2) $I_0 \omega L \sin(\omega t + \pi/2)$ (3) $I_0 \omega L \sin(\omega t - \pi)$ (4) None of these

Q.75 When an AC source of e.m.f. $e = E_0 \sin(100t)$ is connected across a circuit, the phase difference between the e.m.f. e and the current i in the circuit is observed to be $\pi/4$, as shown in the diagram. If the circuit consists possibly only of R-C or R-L or L-C is series, find the relationship between the two elements-

(1) R = 1k Ω , C = 10 μ F (2) R = 1k Ω , C = 1 μ F (3) R = 1k Ω , C = 10H (4) R = 1k Ω , C = 1H

Q.76 A LC circuit is in the state of resonance. If $C = 0.1 \mu F$ and $L = 0.25$ henry. Neglecting ohmic resistance of circuit what is the frequency of oscillations-

Q.77 There is a 5 Ω resistance in an A.C., circuit. Inductance of 0.1 H is connected with it in series. If equation of A.C. e.m.f. is 5 sin 50 t then the phase difference between current and e.m.f. is-

(1)
$$
\frac{\pi}{2}
$$
 (2) $\frac{\pi}{6}$ (3) $\frac{\pi}{4}$ (4) 0

Q.78 An inductor of inductance L and resistor of resistance R are joined in series and connected by a source of frequency ω . Power dissipated in the circuit is-

(1)
$$
\frac{(R^{2} + \omega^{2}L^{2})}{V}
$$

(2)
$$
\frac{V^{2}R}{(R^{2} + \omega^{2}L^{2})}
$$

(3)
$$
\frac{V}{(R^{2} + \omega^{2}L^{2})}
$$

(4)
$$
\frac{\sqrt{R^{2} + \omega^{2}L^{2}}}{V^{2}}
$$

Q.79 In given LCR circuit, the voltage across the terminals of a resistance & current will be-

- **Q.80** In a purely capacitive circuit average power dissipated in the circuit is-
	- (1) V_{rms} I_{rms}
	- (2) Depends on capacitance
	- (3) Infinite
	- (4) Zero
- **Q.81** Phase of current in LCR circuit- (1) Is in the phase potential (2) Leading from the phase of potential (3) Lagging from the phase of potential (4) Before resonance frequency, leading from the phase of potential and after resonance frequency, lagging from the phase of potential **Q.82** In LCR circuit at resonance conditions impedance will be- (1) Equal to R (2) Less than R (3) Greater than R (4) Zero **Q.83** In a circuit having a resistance of 100 Ω connected is series with a capacitive reactance of 100 Ω to an alternating voltage source, the current- (1) Leads voltage by 90º (2) Leads voltage by 45º (3) Lags behind voltage by 90º (4) Lags behind voltage by 45º **Q.84** Which is not correct for capacitive reactance- (1) Resistance of pure capacitor is zero (2) Inversely proportional to frequency (3) Proportional to capacitance (4) Phase difference between voltage and current is 90º **Q.85** The power loss in pure inductor in an A.C. circuit will be- (1) V_{rms} I_{rms} (2) More (3) Zero (4) None of these **Q.86** The hot wire ammeter measures- (1) D.C. current (2) A.C. current (3) None of above (4) both (1) & (2) **Q.87** An AC source of variable frequency is connected to a capacitor C resistor R and inductor L as shown. A is an ammeter. As the frequency is steadily increased the current in A will- **~** A $V \odot \quad \quad C^{\perp}_{\top} \quad \breve{\boxtimes} \mathbb{L} \quad \breve{\geqslant} \mathbb{R}$ (1) go on decreasing gradually
	- (2) go on increasing gradually
	- (3) first increase and then decrease
	- (4) first decrease and then increase

Q.88 200 Ω resistance and 1H inductance are connected in series with an A.C. circuit. The frequency of

the source is 2π $\frac{200}{2}$ Hz. Then phase difference in between V and I will be-

(1) 30º (2) 60º (3) 45º (4) 90º

- **Q.89** In an LCR circuit 10 Ω resistance, 0.5 μ F capacitor and 8 H inductor are connected in series, their angular resonance frequency will be-
	- (1) 800 rad/sec (2) 600 rad/sec (3) 500 rad/sec (4) 300 rad/sec
- **Q.90** In LCR circuit, capacitor C is changed to 4C, then what should be the value of L to keep resonance frequency same- (1) 2 L (2) L/2 (3) L/4 (4) 4L

Q.99 For given parallel circuit correct statement is-

(1) $V = V_R + V_L + V_C$

(2) $I_S = I_R + I_L + I_C$

(3) $I_S < I_R$

(4) value of I_L and I_C may be greater than I_S

Q.100 The power factor of L-R circuit is-

(1)
$$
\frac{\omega L}{R}
$$

\n(2) $\frac{R}{\sqrt{(\omega L)^2 + R^2}}$
\n(3) ωLR
\n(4) $\sqrt{\omega LR}$

Q.101 If alternating current of rms value 'a' flows through resistance R then power loss in resistance is- (1) zero $(2) a²R$

$$
(3) \frac{a^2 R}{2} \qquad (4) 2a^2 R
$$

Q.102 For an alternating current of frequency π 500 Hz in L-C-R series circuit with $L = 1H$, $C = 1\mu F$,

 $R = 100\Omega$. impedance is-

(1) 100 Ω $100\sqrt{\pi} \Omega$

- (3) $100\sqrt{2\pi}$ (4) 100 $\pi\Omega$
- **Q.103** Which of the following device in alternating circuit provides maximum power-

(1) Only capacitor

(2) Capacitor and resistor

(3) Only inductor

(4) Only resistor

Q.104 If an alternating current $i = i_m$ sinot is flowing through a capacitor then voltage drop ΔV_c across capacitor C will be ?

$$
(1) - \frac{i_{\text{m}}}{\omega C} \sin \omega t
$$

$$
(2) - \frac{i_{\text{m}}}{\omega C} \cos \omega t
$$

$$
(3) - \frac{i_{\text{m}}}{\omega C} \left(\sin \omega t + \frac{\pi}{4} \right)
$$

$$
(4) \frac{i_{\text{m}}}{\omega C} \left(\sin \omega t - \frac{\pi}{4} \right)
$$

Q.105 If alternating current of 60 Hz frequency is flowing through inductance of L = 1 mH and drop in ΔV_L is 0.6 V then alternating current-

(1)
$$
\frac{1}{\pi}
$$
A (2) $\frac{5}{\pi}$ A (3) $\frac{50}{\pi}$ A (4) $\frac{20}{\pi}$ A

Q.106 For an alternating current $I = I_0 \cos \omega t$, what is the rms value and peak value of current-

(1)
$$
I_0
$$
, $\frac{I_0}{\sqrt{2}}$
\n(2) $\frac{I_0}{\sqrt{2}}$, I_0
\n(3) I_0 , $\frac{I_0}{\sqrt{2}}$
\n(4) $2I_0$, $\frac{I_0}{\sqrt{2}}$

Q.107 If an alternating current $i = i_m$ sin ω t is flowing through an inductor then voltage drop ΔV_1 across inductor L will be-

(1) $i_m \omega L \sin \omega t$ (2) $i_m \omega L \cos \omega t$ (3) i_m ω L sin ω t + $\frac{\pi}{4}$ J $\left(\omega t+\frac{\pi}{t}\right)$ J $\left(\omega t + \frac{\pi}{4}\right)$ (4) i_m ω L cos $\left(\omega t - \frac{\pi}{4}\right)$ $\left(\omega t - \frac{\pi}{t}\right)$ Y $\left(\omega t - \frac{\pi}{4}\right)$

Q.108 If frequency of alternating source is made zero then which of the following statement is true-(1) current through capacitor will be zero

J

- (2) current through resistance will be zero
- (3) current through inductance will be zero
- (4) all
- **Q.109** The power factor of an A.C. circuit having resistance (R) and inductance (L) connected in series and an angular velocity ω is -

(1)
$$
\frac{R}{\omega L}
$$

\n(2) $\frac{R}{(R^2 + \omega^2 L^2)^{1/2}}$
\n(3) $\frac{\omega L}{R}$
\n(4) $\frac{R}{(R^2 - \omega^2 L^2)^{1/2}}$

Q.110 Power factor of the circuit is –

R	L
www	0000000
$\varepsilon = \varepsilon_0 \sin \omega t$	
R	$\varepsilon = 2.123272$

$$
(1) \frac{\mathrm{R}}{\omega \mathrm{L}}
$$

$$
(2) \frac{R}{\sqrt{R^2 + \omega^2 L^2}}
$$

(3)
$$
\frac{R}{R^2 + \omega^2 L^2}
$$
 (4) none of these

- **Q.111** Alternating current can not be measured by D.C. ammeter because
	- (1) A.C. can not pass through D.C. Ammeter
	- (2) A.C. changes direction
	- (3) Average value of current for complete cycle is zero
	- (4) D.C. Ammeter will get damaged
- **Q.112** In an LCR series a.c. circuit, the voltage across each of the components, L, C and R is 50 V. The voltage across the LC combination will be -

- **Q.113** In a LCR circuit capacitance is changed from C to 2C. For the resonant frequency to remain unchanged, the inductance should be changed from L to -
	- (1) 4 L (2) 2 L $(3) L/2$ (4) $L/4$
- **Q.114** The self inductance of the motor of an electric fan is 10 H. In order to impart maximum power at 50 Hz, it should be connected to a capacitance of – **** (1) 4uF (2) 8uF (3) 1uF (4) 2uF

Q.115 A circuit has a resistance of 12 ohm and an impedance of 15 ohm. The power factor of the circuit will be -

(1) 0.8 (2) 0.4 (3) 1.25 (4) 0.125

- **Q.116** The phase difference between the alternating current and emf is $\pi/2$. Which of the following cannot be the constituent of the circuit ? (1) C alone (2) R L (3) L C (4) L alone
- **Q.117** In a series resonant LCR circuit, the voltage across R is 100 volts and R = 1 k Ω with C = 2 µF. The resonant frequency ω is 200 rad/s. At resonance the voltage across L is -
	- (1) 250 V (2) 4×10^{-3} V (3) 2.5 \times 10⁻² V (4) 40 V
- **Q.118** In an a.c. circuit the voltage applied is $E = E_0$ sin ω t. The resulting current in the circuit is $I = I_0$ sin

$$
\left(\omega t - \frac{\pi}{2}\right)
$$
. The power consumption in the circuit is given by -
(1) P = $\frac{E_0 I_0}{\sqrt{2}}$ (2) P = zero
(3) P = $\frac{E_0 I_0}{2}$ (4) P = $\sqrt{2}$ E₀I₀

Q.119 An inductor of inductance L = 400 mH and resistors of resistances R₁ = 2 Ω and R₂ = 2 Ω are connected to a battery of emf 12V as shown in the figure. The internal resistance of the battery is negligible. The switch S is closed at $t = 0$. The potential drop across L as a function of time is $-$

Q.120 In a series LCR circuit R = 200 Ω and the voltage and the frequency of the main supply is 220 V and 50 Hz respectively. On taking out the capacitance from the circuit the current lags behind the voltage by 30°. On taking out the inductor from the circuit the current leads the voltage by 30°. The power dissipated in the LCR circuit is $-$

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